Refinements for Session-typed Concurrency

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- Processes represented as nodes
- Channels between processes as edges
- Each channel is "provided" by a specific process (P provides c, Q provides d etc.)

- Processes compute internally
- Exchange messages along channels



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• Processes can also send channels they own



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- Don't want to send int if expecting string
- Don't try to receive if other process is not sending
- Assign types to each channel from provider's perspective



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Linear Session Types

• Example interface specification:

```
queue = &{enq: A -o queue,
      deq: ⊕{none: 1, some: A ⊗ queue}}
* where A is some predetermined type
```

1	Terminate
$\{lab_i:A_i\}_i$	External choice (receive) between lab _i , continue as A _i
А — о В	Receive channel of type A, continue as B
Τ⊃B	Receive value of type τ, continue as B
$\oplus \{ lab_i: A_i \}_i$	Internal choice (send) between lab _i , continue as A _i
А 🛛 В	Send channel of type A, continue as B
т∧ В	Send value of type τ, continue as B

Implementation of Queues

```
queue = \&\{enq: A - o queue, 
                deq: \oplus {none: 1, some: A \otimes queue}}
empty : queue
q ← empty =
   case q
      enq \rightarrow x \leftarrow recv q;
                  e \leftarrow empty;
                  q \leftarrow \text{elem } \mathbf{x} \in
      deq \rightarrow q.none; close q
elem : A -o queue -o queue
q \leftarrow \text{elem } \mathbf{x} \mathbf{r} =
   case q
      enq \rightarrow y \leftarrow recv q;
                  r.enq ; send r y ;
                  q \leftarrow \text{elem } \mathbf{x} \mathbf{r}
      deq \rightarrow q.some ; send q x ;
                  q \leftarrow r
```

Intersections and Unions

- Allows describing more interesting behavior
- Intersection of two types: A ⊓ B
 − c : A ⊓ B if channel c offers both behaviors
- Union of two types: A ⊔ B

– c : A \sqcup B if channel c offers either behavior

Refinement Types

- What if we want to track more properties of queues? Empty, non-empty, even length?
- We can define them in the base system:

Refinement Types

 But we need intersections and unions to write interesting programs

```
queue A = empty-queue □ nonempty-queue
empty : empty-queue
elem : (A -o queue -o nonempty-queue)
concat : (empty-queue -o empty-queue -o empty-queue)
□ (queue -o nonempty-queue -o nonempty-queue)
□ (nonempty-queue -o queue -o nonempty-queue)
```

Decidability of Type-checking

- Algorithmic system that is easy to translate to code
- Prove sound and complete with respect to the original system
- Partial implementation in Haskell

Type Safety

- Progress
 - Deadlock freedom in concurrent setting
 - At least one process can make progress if the configuration is well-typed
- Preservation [currently in progress]
 - Session fidelity in concurrent setting
 - Processes obey session-types