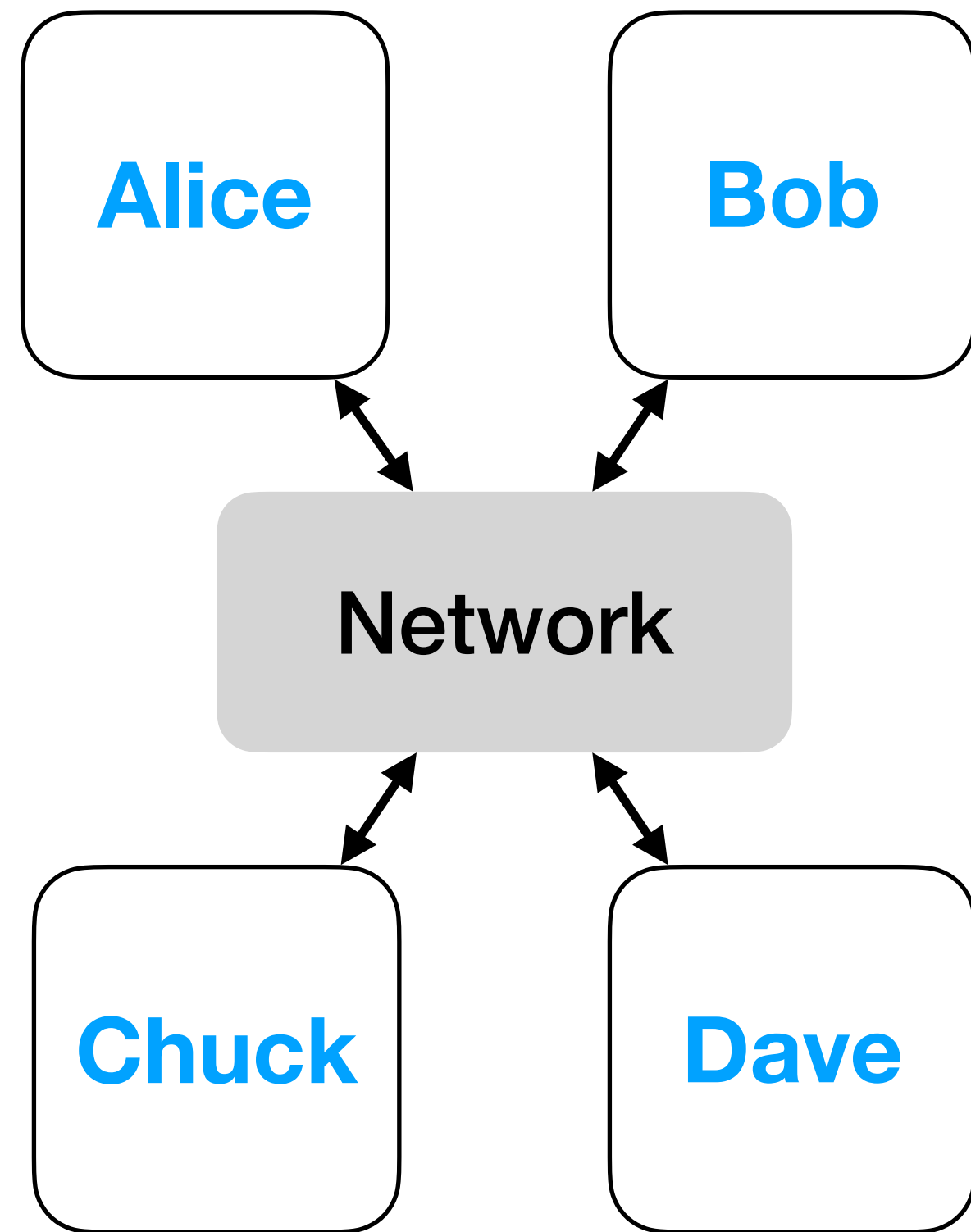


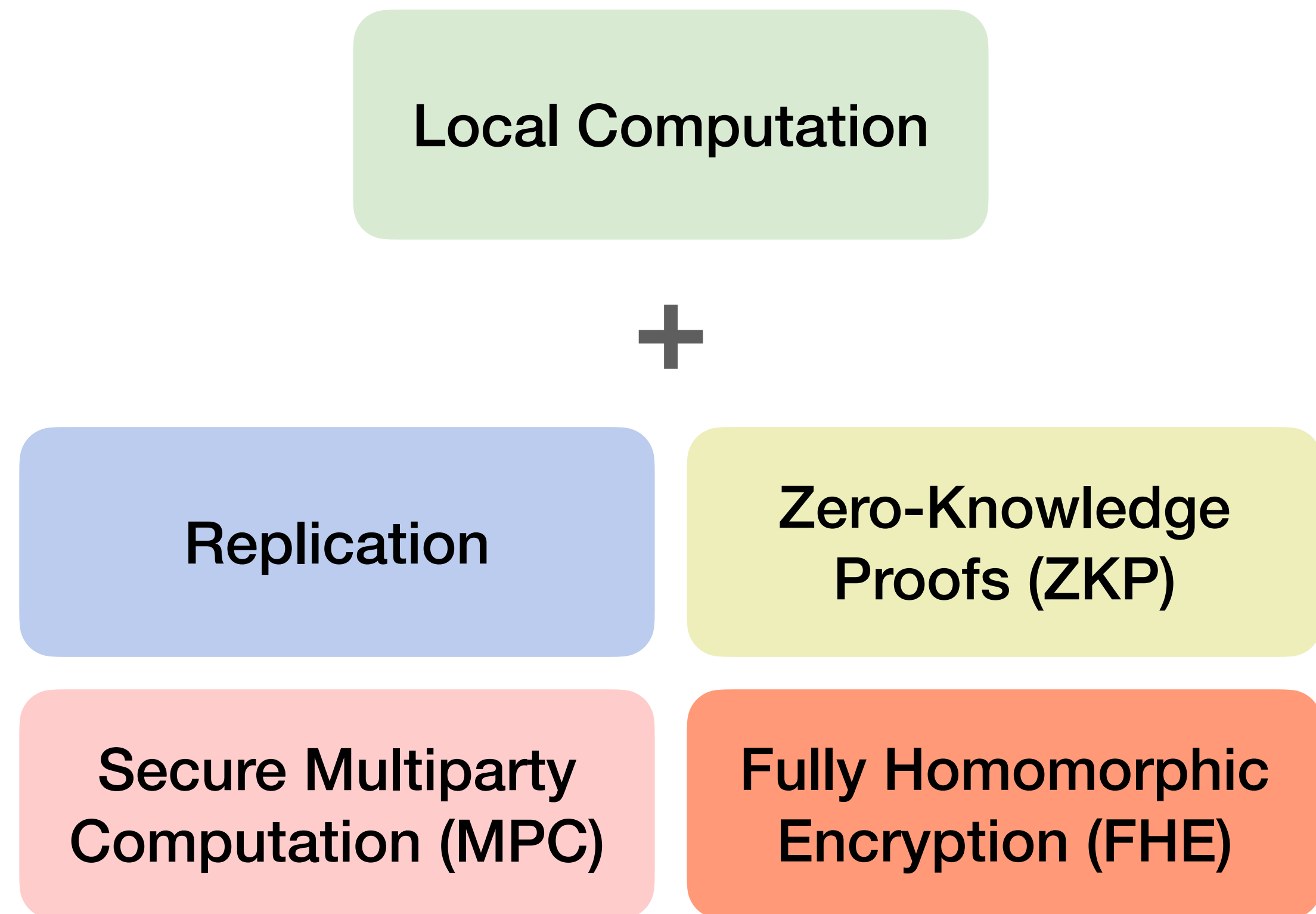
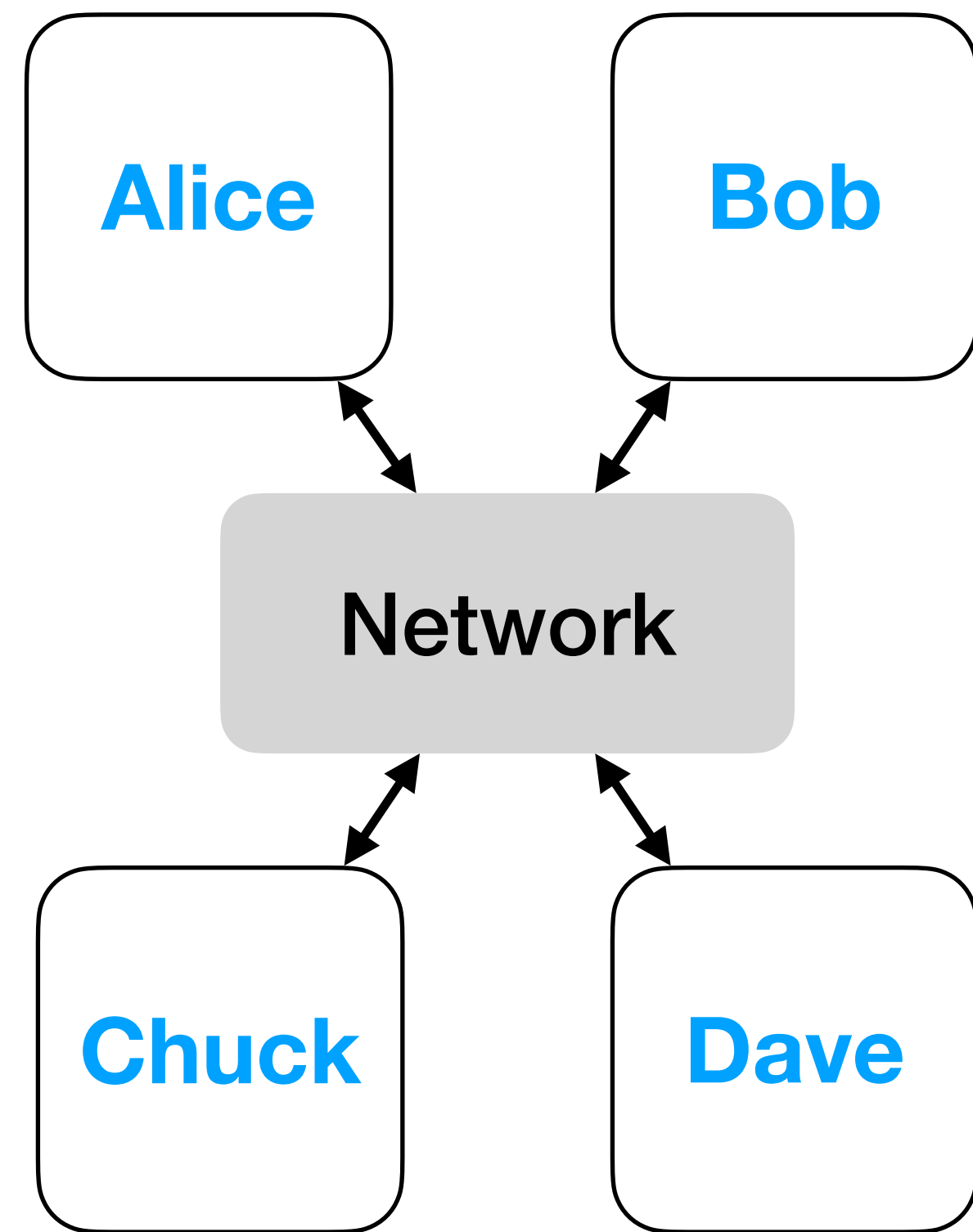
# **Provably Correct Compilation for Distributed Cryptographic Applications**

**Josh Acay — July 19, 2023**

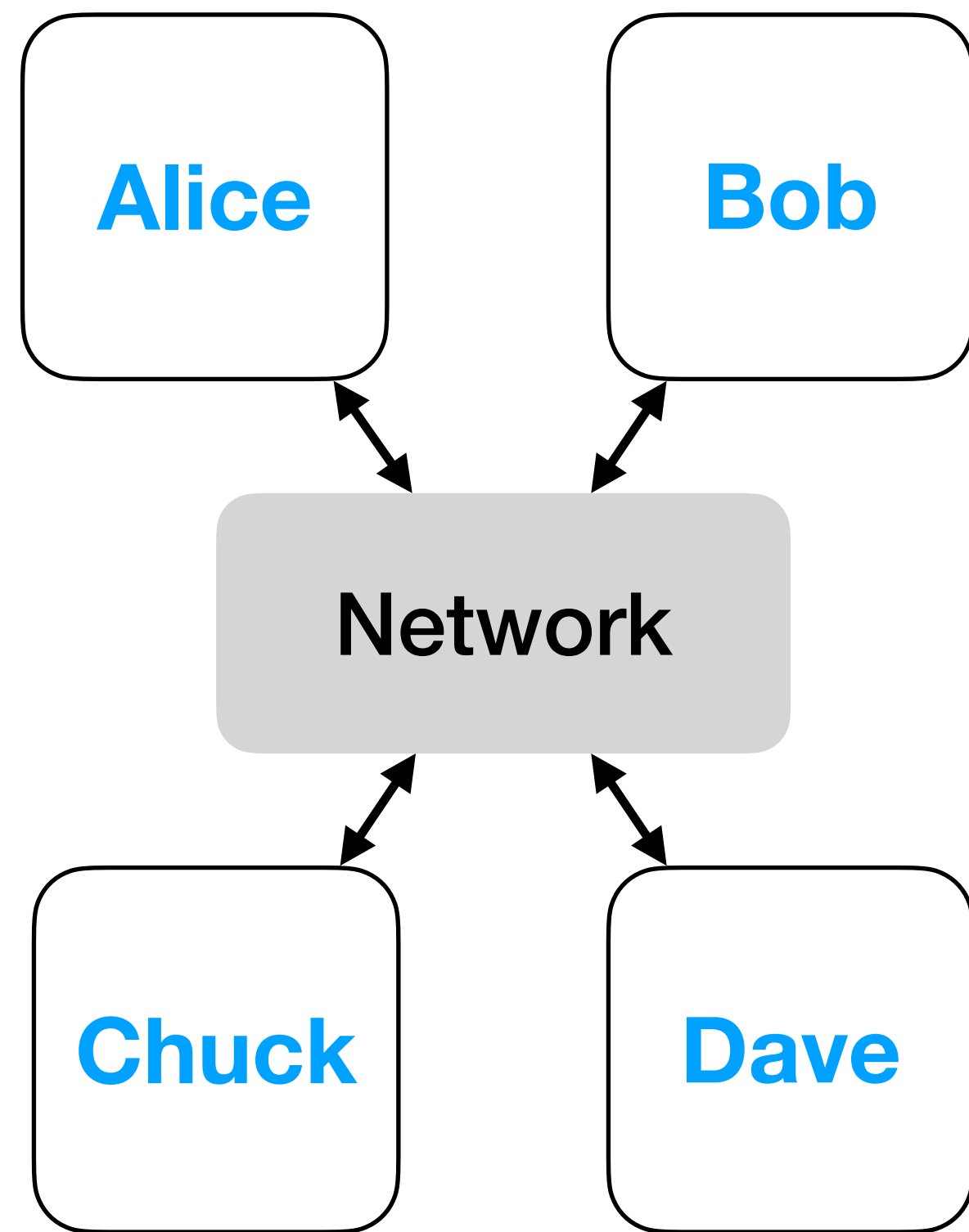
# Secure Distributed Applications



# Secure Distributed Applications



# Secure Distributed Applications



Local Computation

+

Replication

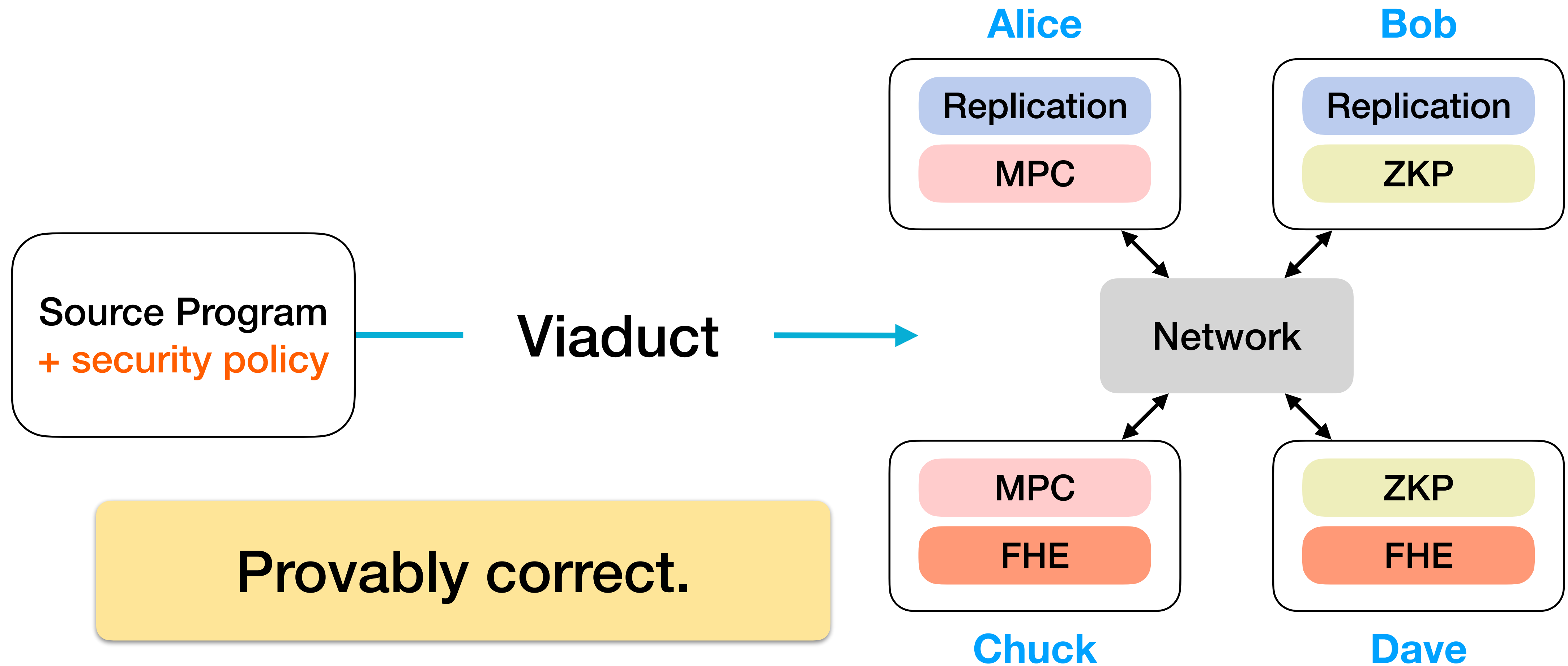
Zero-Knowledge Proofs (ZKP)

Secure Multiparty Computation (MPC)

Fully Homomorphic Encryption (FHE)

**Difficult and error prone.**

# Viaduct: Let the Compiler Worry About Cryptography



# Leaked Password Checking

**Browser**

User Passwords

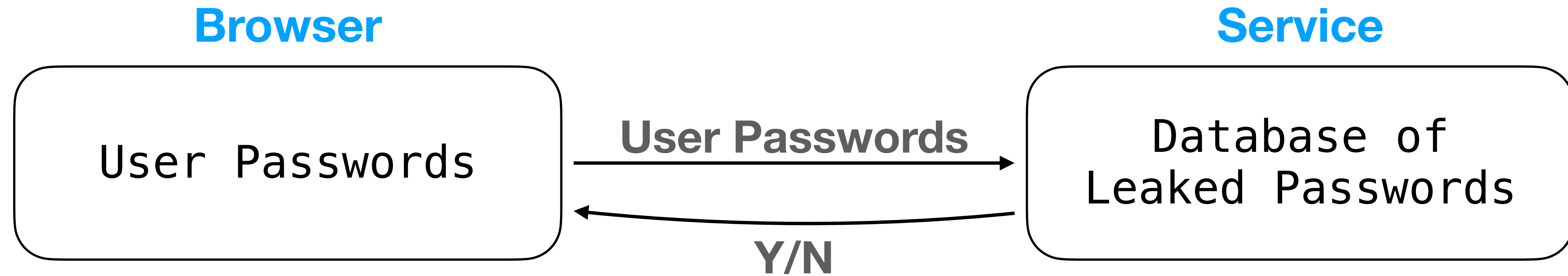
**Service**

Database of  
Leaked Passwords

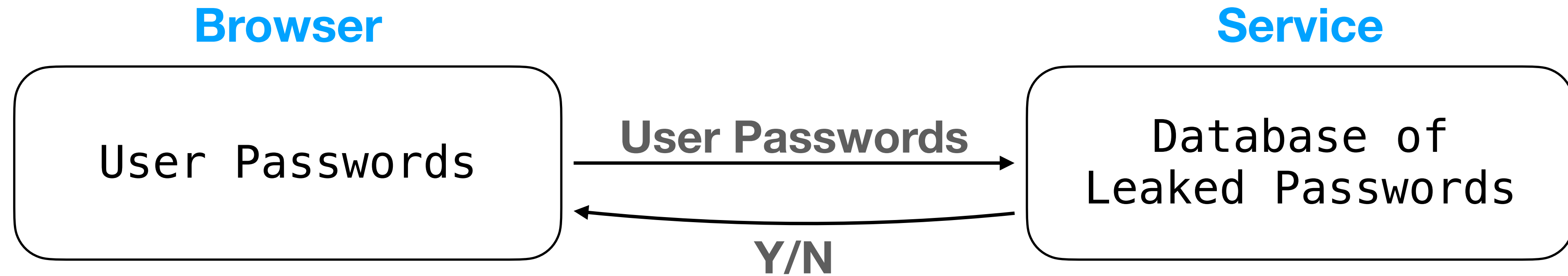
**Service** has a database of leaked passwords.

**Browser** wants to know if passwords are compromised.

# Server-Side Computation is Insecure



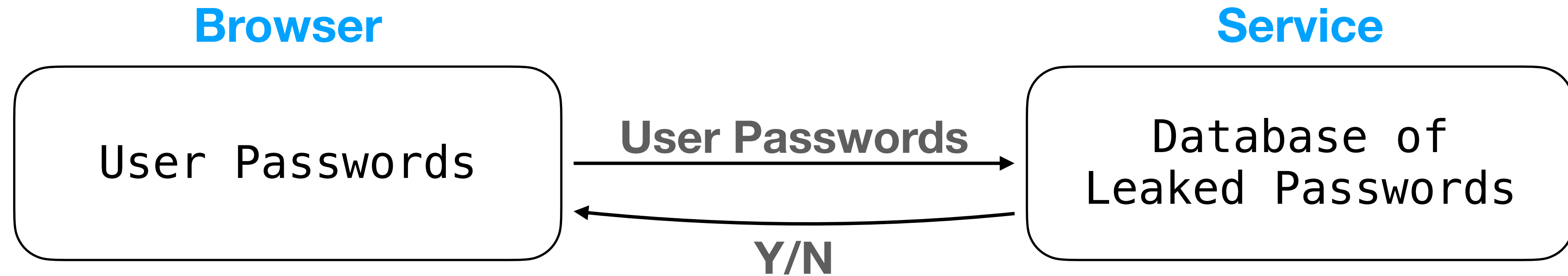
# Server-Side Computation is Insecure



**Service** learns user passwords!



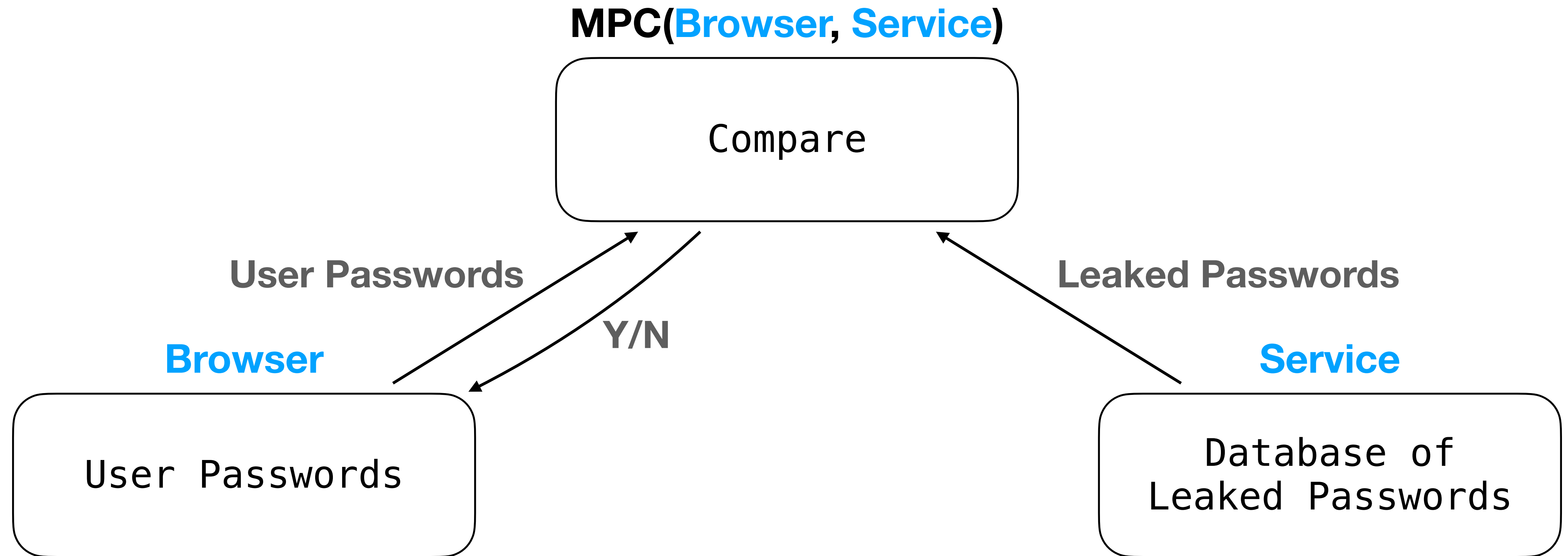
# Server-Side Computation is Insecure



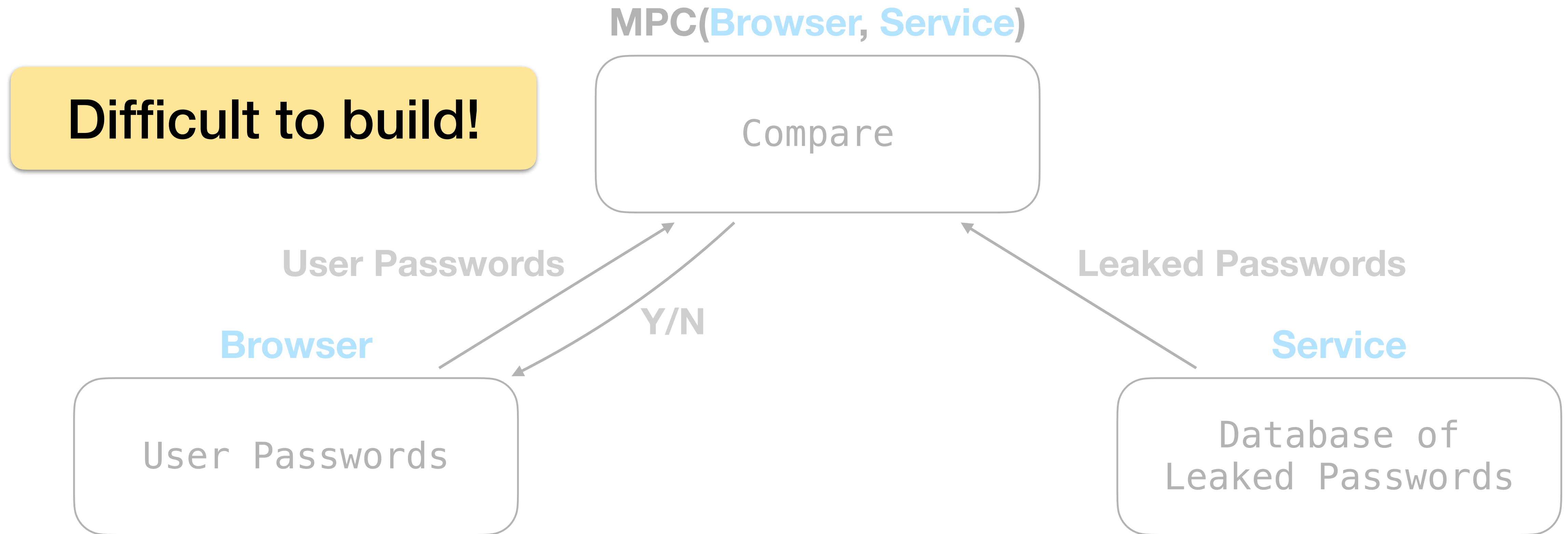
**Service** learns user passwords!

Sending database to **Browser** is not secure either.

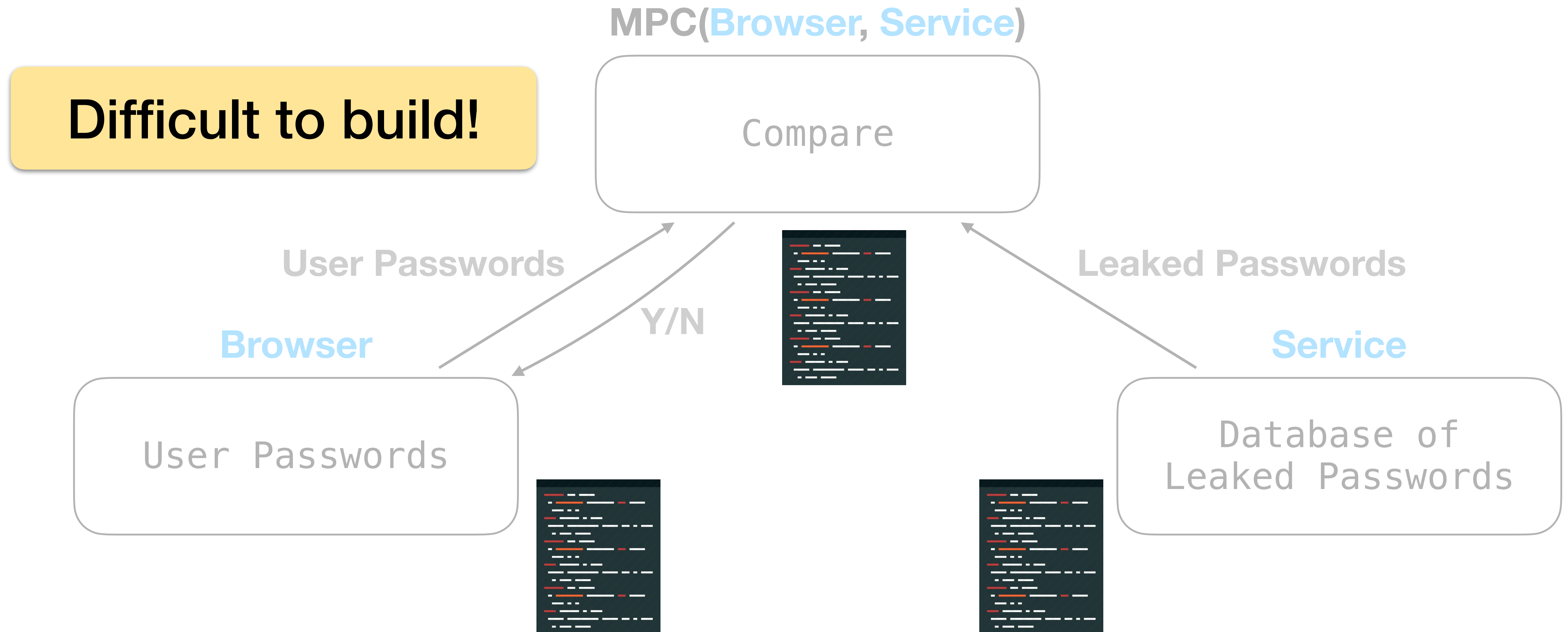
# Need Cryptography for Security



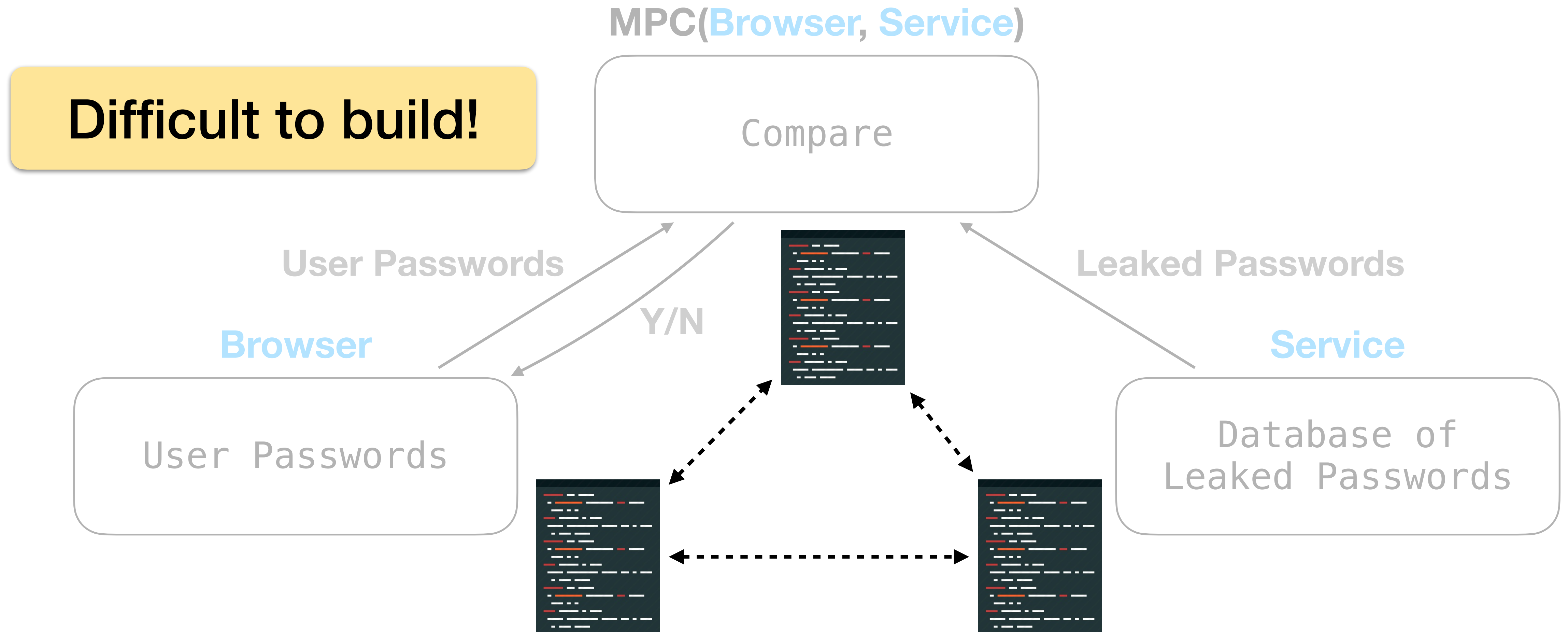
# Need Cryptography for Security



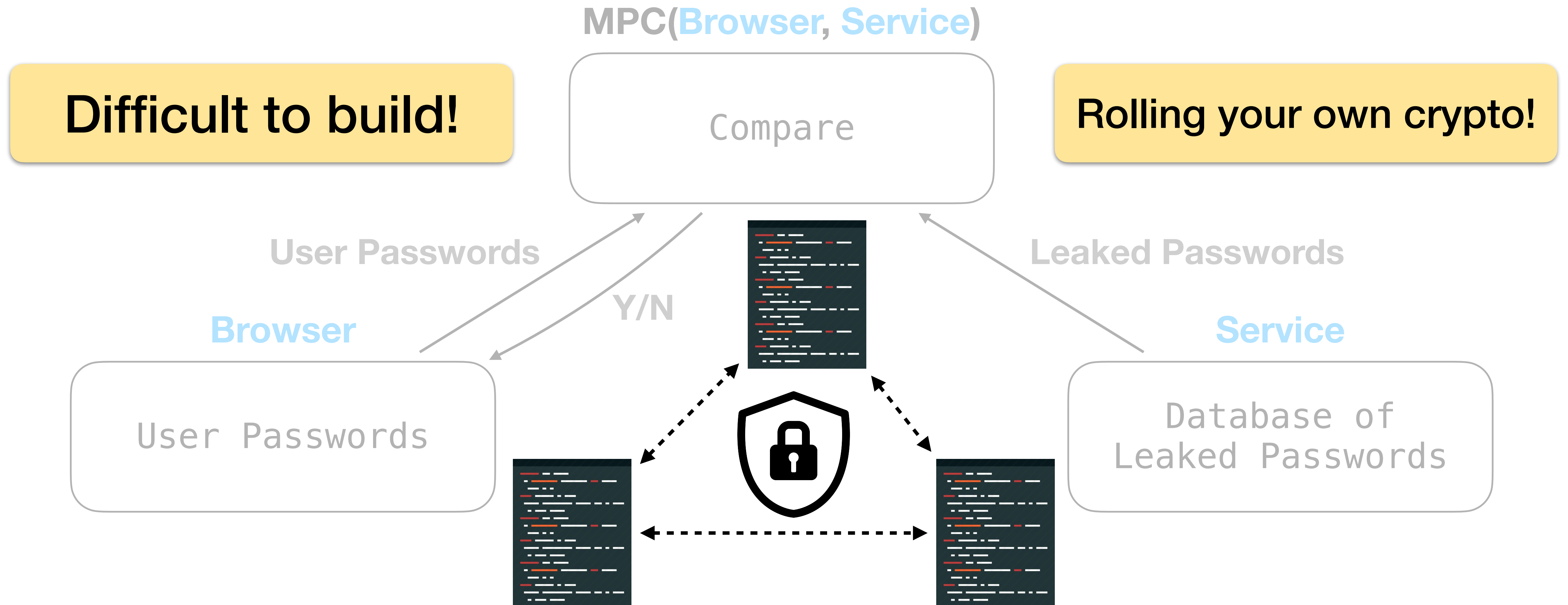
# Need Cryptography for Security



# Need Cryptography for Security



# Need Cryptography for Security



# The Viaduct Approach

```
host Browser  
host Service
```

```
fun check_passwords() {  
    val b = Browser.input<int>()  
    val s = Service.input<Array<int>>()  
    val leaked = b ∈ s  
    Browser.output(leaked)  
}
```

# The Viaduct Approach

```
host Browser  
host Service
```

```
fun check_passwords() {  
    val b = Browser.input<int>()  
    val s = Service.input<Array<int>>()  
    val leaked = b ∈ s  
    Browser.output(leaked)  
}
```

Single program

Sequential

Doesn't mention crypto



# Viaduct Synthesizes Secure Protocols


```
host Browser  
host Service
```

```
fun check_passwords() {  
    val b@Browser = Browser.input<int>()  
    val s@Service = Service.input<Array<int>>()  
    val leaked@MPC(Browser, Service) = b ∈ s  
    Browser.output(leaked)  
}
```

# Viaduct Synthesizes Secure Protocols

```
host Browser
host Service
```

How does Viaduct  
decide this needs  
cryptography?



```
fun check_passwords() {
  val b@Browser = Browser.input<int>()
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# Viaduct Synthesizes Secure Protocols

```
host Browser
host Service
```

```
fun check_passwords() {
  val b@Browser = Browser.input<int>()
  val s@Service = Service.input<Array<int>>()
  val leaked@MPC(Browser, Service) = b € s
  Browser.output(leaked)
}
```

How does Viaduct  
decide this needs  
cryptography?



Intutively, involves  
data from both hosts.

# Viaduct Synthesizes Secure Protocols

```
host Browser  
host Service
```

How does Viaduct  
decide this needs  
cryptography?

```
fun check_passwords() {  
  va  
  va  
  val leaked@mPC(Browser, Service) = D ∈ S  
  Browser.output(leaked)  
}
```

We need a way to formally specify security policies.

Intutively, involves  
data from both hosts.

# Information Flow Labels

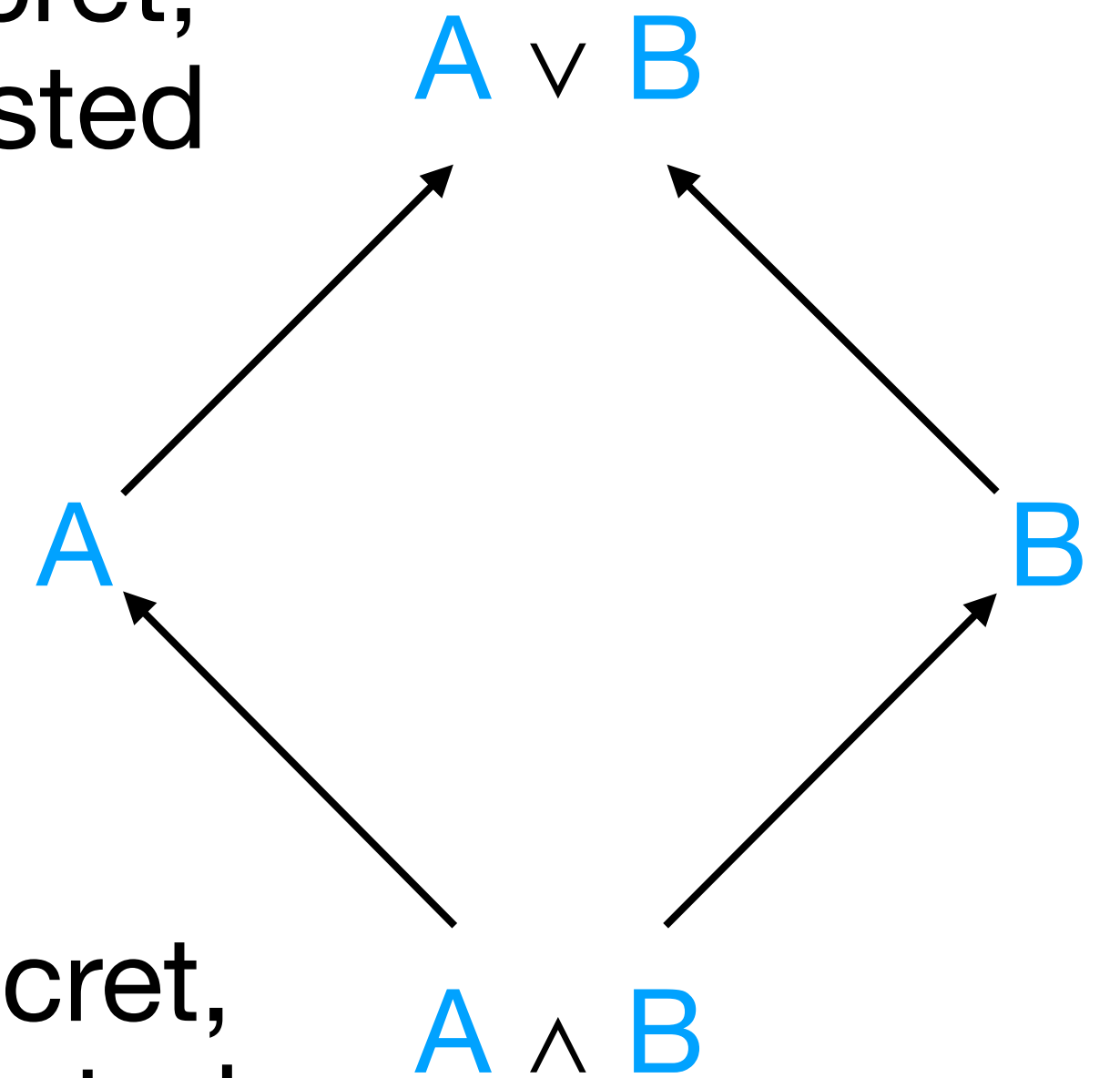
Pair of confidentiality and integrity:

$$\ell = \langle \textit{confidentiality}, \textit{integrity} \rangle$$

Each component a boolean formula over **hosts**

Ordered by implication:  $A \wedge B \Rightarrow A \Rightarrow A \vee B$

**less** secret,  
**less** trusted



**more** secret,  
**more** trusted

# Data Labels (Standard Information Flow Typing)

```
fun check_passwords() {  
    val b : ⟨Browser, Browser⟩ = Browser.input<int>()  
}
```

# Data Labels (Standard Information Flow Typing)

```
fun check_passwords() {  
    val b : ⟨Browser, Browser⟩ = Browser.input<int>()  
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}
```

# Data Labels (Standard Information Flow Typing)

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fun check_passwords() {  
  val b : ⟨Browser, Browser⟩ = Browser.input<int>()  
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  val leaked : ⟨B ∧ S, B ∨ S⟩ = b ∈ s
```



# Data Labels (Standard Information Flow Typing)

```
fun check_passwords() {  
    val b : ⟨Browser, Browser⟩ = Browser.input<int>()  
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    Browser.output(leaked)
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fun check_passwords() {  
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    val leaked : ⟨B ∧ S, B ∨ S⟩ = b ∈ s  
    Browser.output(leaked)
```

Check:

- leaked has *less confidentiality* than Browser
- leaked has *more integrity* than Browser
- $\langle B \wedge S, B \vee S \rangle \sqsubseteq \langle B, B \rangle$

# Data Labels (Standard Information Flow Typing)

```
fun check_passwords() {  
  val b : ⟨Browser, Browser⟩ = Browser.input<int>()  
  val s : ⟨Service, Service⟩ = Service.input<Array<int>>()  
  val leaked : ⟨B ∧ S, B ∨ S⟩ = b ∈ s
```

`Browser.output(leaked)`

Check:

- leaked has *less confidentiality* than Browser
- leaked has *more integrity* than Browser
- $\langle B \wedge S, B \vee S \rangle \sqsubseteq \langle B, B \rangle$

**Both checks fail!**

# Downgrades Specify Intended Security Policy

```
fun check_passwords() {  
  val b :  $\langle B, B \wedge S \rangle$  = endorse(Browser.input(), Service)  
  val s :  $\langle B, B \wedge S \rangle$  = endorse(Service.input(), Browser)  
  val leaked :  $\langle B \wedge S, B \wedge S \rangle$  = b ∈ s  
  val leaked' :  $\langle B, B \wedge S \rangle$  = declassify(leaked, Browser)  
  Browser.output(leaked')  
}
```

# Downgrades Specify Intended Security Policy

```
fun check_passwords() {  
  val b :  $\langle B, B \wedge S \rangle$  = endorse(Browser.input(), Service)  
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}
```

“I know this reveals some data to Browser. That’s intended.”

# Downgrades Specify Intended Security Policy

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fun check_passwords() {  
    val b : ⟨B, B ∧ S⟩ = endorse(Browser.input(), Service)  
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    val leaked : ⟨B ∧ S, B ∧ S⟩ = b ∈ s  
    val leaked' : ⟨B, B ∧ S⟩ = declassify(leaked, Browser)  
    Browser.output(leaked')  
}
```

“Service/Browser accepts this data,  
whatever it is.”

“I know this reveals some data to  
Browser. That’s intended.”

***Data*** labels specify confidentiality/integrity ***requirements***.

Assign labels to ***hosts*** to capture confidentiality/integrity ***guarantees***.

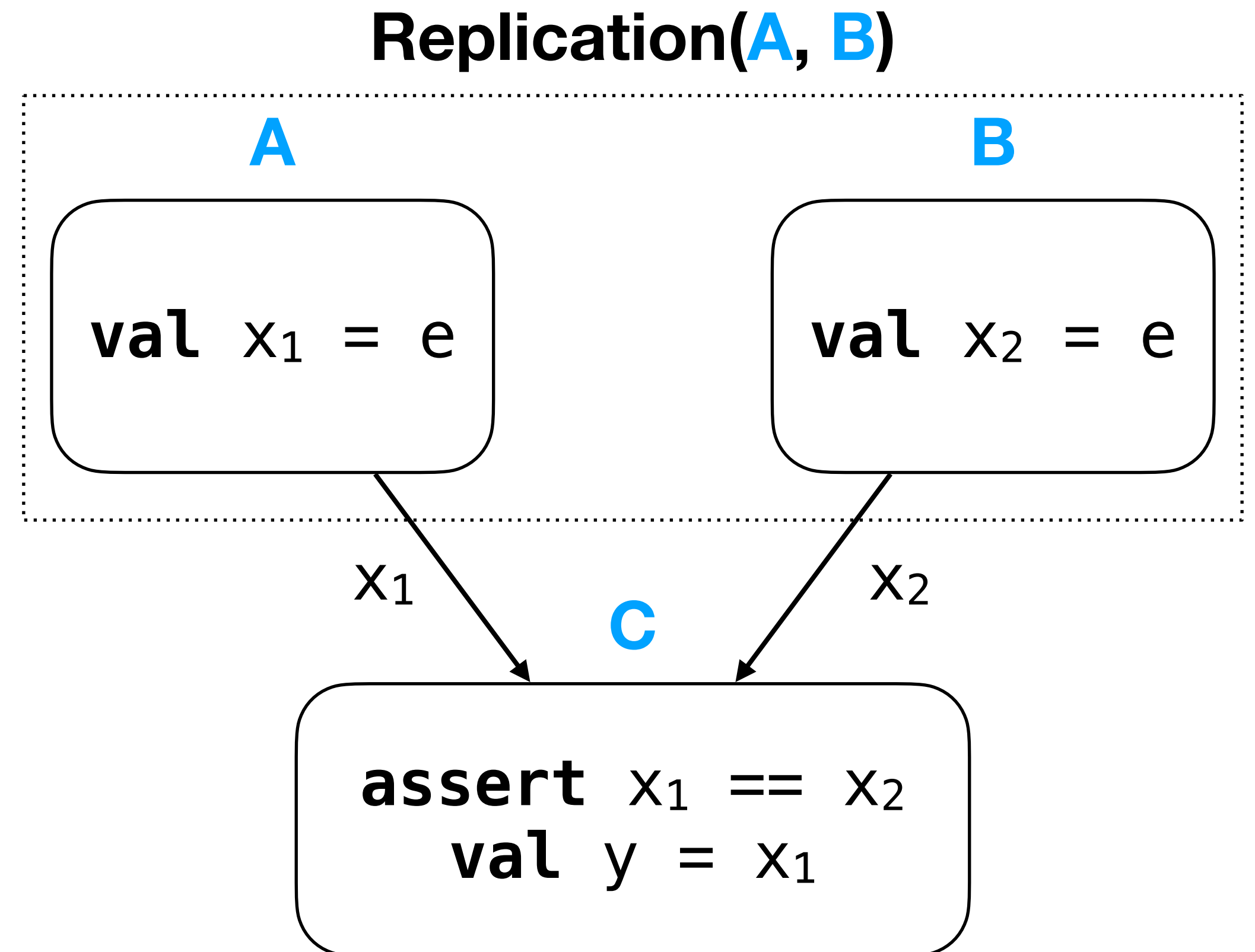
# Replication

**val**  $x@Replication(A, B) = e$

**val**  $y@C = x$

- Computation and storage replicated
- Verify all replicas are consistent
- Low confidentiality, high integrity:

$label(Replication(A, B)) = \langle A \vee B, A \wedge B \rangle$





# Host Labels

---

Host	Confidentiality	Integrity
$h$	$h$	$h$
Replication( $h_1, h_2$ )	$h_1 \vee h_2$	$h_1 \wedge h_2$

---

# Host Labels

---

Host	Confidentiality	Integrity
$h$	$h$	$h$
Replication( $h_1, h_2$ )	$h_1 \vee h_2$	$h_1 \wedge h_2$
MPC( $h_1, h_2$ )	$h_1 \wedge h_2$	$h_1 \wedge h_2$

---

# Host Labels

Host	Confidentiality	Integrity
$h$	$h$	$h$
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Semi-honest MPC( $h_1, h_2$ )	$h_1 \wedge h_2$	$h_1 \vee h_2$

# Host Labels

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Commitment( $p, v$ )	$p$	$p \wedge v$

# Host Labels

---

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Replication( $h_1, h_2$ )	$h_1 \vee h_2$	$h_1 \wedge h_2$
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Commitment( $p, v$ )	$p$	$p \wedge v$
ZKP( $p, v$ )	$p$	$p \wedge v$

---

# Connecting Data and Host Labels

- A host can perform a computation if it has higher confidentiality & integrity:

$$\text{label}(\text{host}) \Rightarrow \text{label}(\text{variable})$$

$$\text{val } a@A : \langle A, A \rangle = \dots$$

$$\text{val } b@A : \langle A \vee B, A \rangle = \dots$$

$$\text{val } c@A : \langle A \wedge B, A \rangle = \dots$$

$$\text{val } d@MPC(A, B) : \langle A \wedge B, A \wedge B \rangle = \dots$$

$$\text{label}(A) = \langle A, A \rangle$$

$$\text{label}(MPC(A, B)) = \langle A \wedge B, A \wedge B \rangle$$

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- A host can perform a computation if it has higher confidentiality & integrity:

label(host)  $\Rightarrow$  label(variable)

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label(A) =  $\langle A, A \rangle$   
label(MPC(A, B)) =  $\langle A \wedge B, A \wedge B \rangle$

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$$\text{val } c@A : \langle A \wedge B, A \rangle = \dots$$

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--



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$\text{label}(A) = \langle A, A \rangle$ $\text{label}(\text{MPC}(A, B)) = \langle A \wedge B, A \wedge B \rangle$
--

# Cost Model & Optimal Host Selection

- Labels eliminate insecure host assignments
- This still leaves multiple valid host assignments
- Viaduct solves an optimization problem based on a cost model
  - Avoid MPC and ZKP; prefer Local and Replication
  - Minimize data movement between hosts

# Underdetermined Protocol

```
fun check_passwords() {  
    val b@Browser = endorse(Browser.input(), Service)  
    val s@Service = endorse(Service.input(), Browser)  
    val leaked@MPC(Browser, Service) = b ∈ s  
    val leaked'@MPC(B..., S...) = declassify(leaked, Browser)  
    Browser.output(leaked')  
}
```

# Underdetermined Protocol

```
fun check_passwords() {  
  val b@Browser = endorse(Browser.input(), Service)  
  val s@Service = endorse(Service.input(), Browser)  
  val leaked@MPC(Browser, Service) = b ∈ s  
  val leaked'@MPC(B..., S...) = declassify(leaked, Browser)  
  Browser.output(leaked')  
}
```

Implicit communication

# Choreographies: Manifesting Communication

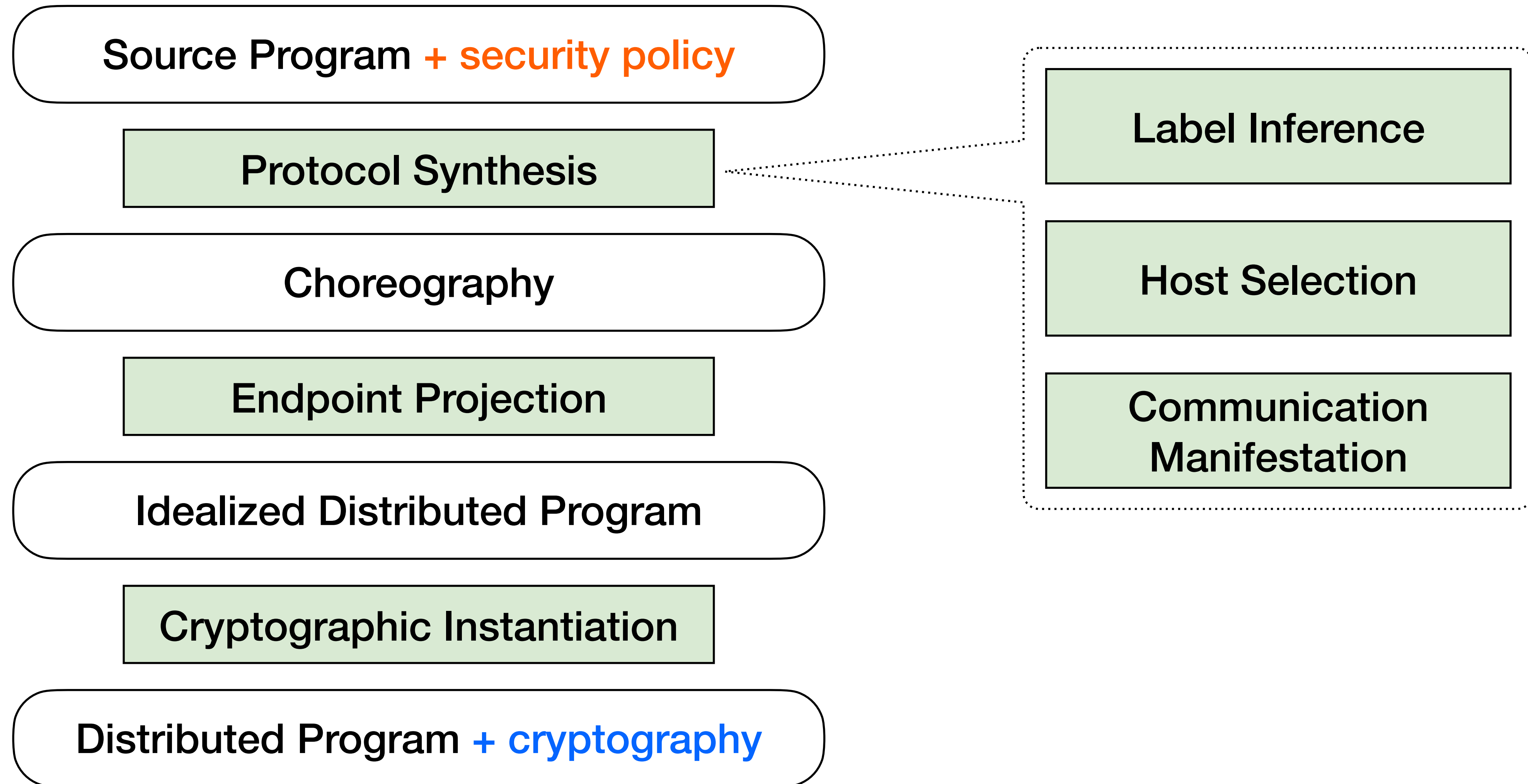
```
fun check_passwords() {  
  val b@Browser = endorse(Browser.input(), Service)  
  Browser.b  $\rightsquigarrow$  MPC(Browser, Service).b'  
  val s@Service = endorse(Service.input(), Browser)  
  Service.s  $\rightsquigarrow$  MPC(Browser, Service).s'  
  val leaked@MPC(Browser, Service) = b'  $\in$  s'  
  val leaked'@MPC(B..., S...) = declassify(leaked, Browser)  
  MPC(Browser, Service).leaked'  $\rightsquigarrow$  Browser.leaked''  
  Browser.output(leaked'')  
}
```

# Choreographies: Manifesting Communication

```
fun check_passwords() {  
    val b@Browser = endorse(Browser.input(), Service)  
    Browser.b ↗ MPC(Browser, Service).b'  
    val s@Service = endorse(Service.input(), Browser)  
    Service.s ↗ MPC(Browser, Service).s'  
    val leaked@MPC(Browser, Service) = b' ∈ s'  
    val leaked'@MPC(B..., S...) = declassify(leaked, Browser)  
    MPC(Browser, Service).leaked' ↗ Browser.leaked''  
    Browser.output(leaked'')  
}
```

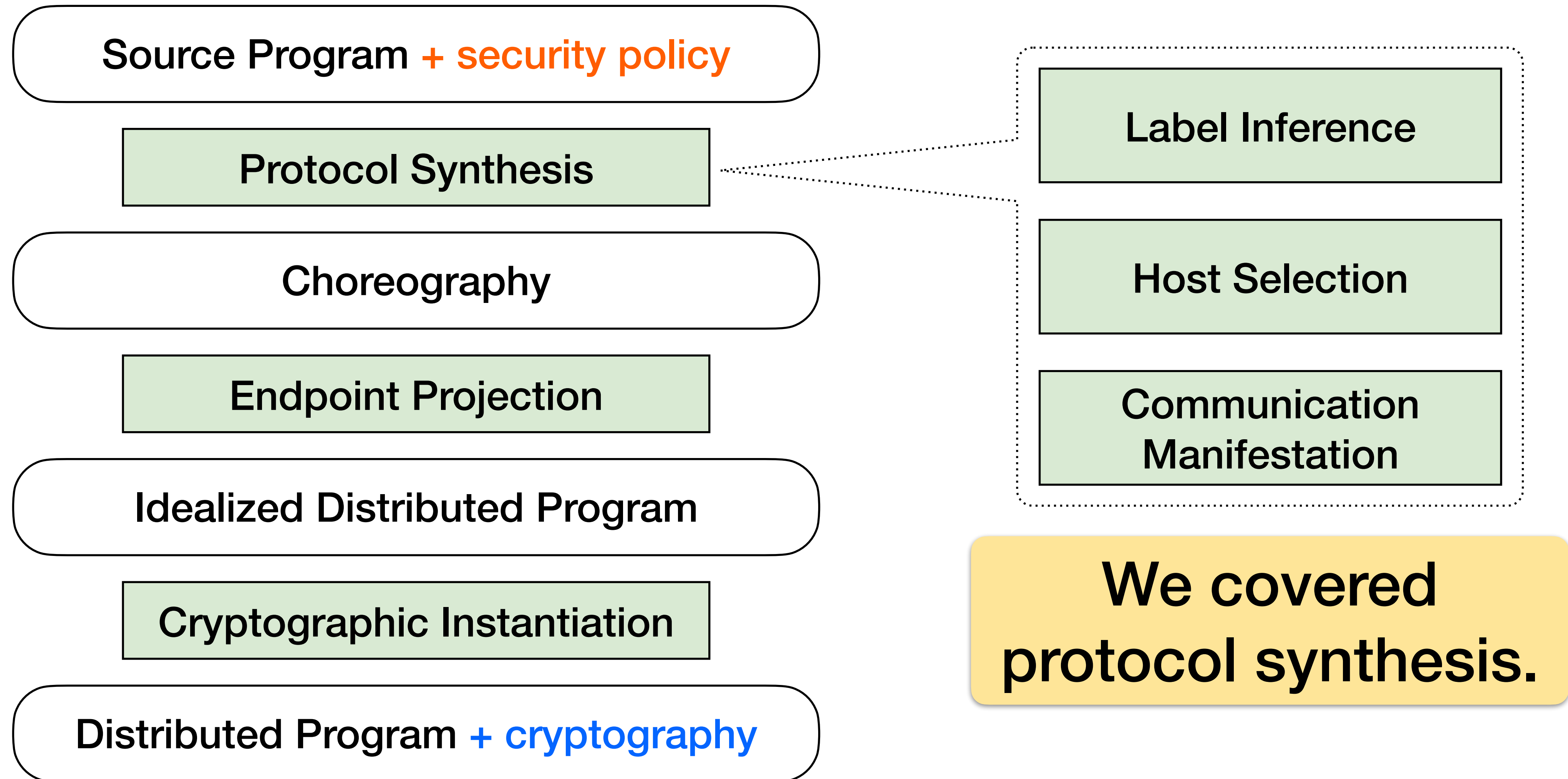
Multiple ways of inserting communication events.

# Compilation Overview





# Compilation Overview



# Endpoint Projection

## Choreography

```
val b@Browser = Browser.input()  
Browser.b ↔ MPC(B..., S...).b'  
...  
Browser.output('leaked')
```

project **Browser**

project MPC

project **Service**

```
val b = input()  
send b to MPC(B..., S...)  
...  
output('leaked')
```

**Browser**

```
val b' = receive B...  
...
```

**MPC(Browser, Service)**

...

**Service**

# Endpoint Projection

## Choreography

```
→ val b@Browser = Browser.input()  
   Browser.b ⇔ MPC(B..., S...).b'  
   ...  
   Browser.output('leaked')
```

project **Browser**

project MPC

project **Service**

```
→ val b = input()  
   send b to MPC(B..., S...)  
   ...  
   output('leaked')
```

**Browser**

```
→ val b' = receive B...  
   ...
```

**MPC(Browser, Service)**

```
→ ...
```

**Service**

# Endpoint Projection

## Choreography

```
val b@Browser = Browser.input()  
Browser.b ↔ MPC(B..., S...).b'  
...  
Browser.output('leaked')
```

project **Browser**

project **MPC**

project **Service**

```
val b = input()  
send b to MPC(B..., S...)  
...  
output('leaked')
```

**Browser**

```
val b' = receive B...  
...
```

**MPC(Browser, Service)**

```
...
```

**Service**

# Endpoint Projection

## Choreography

```
val b@Browser = Browser.input()  
Browser.b ↔ MPC(B..., S...).b'  
...  
Browser.output('leaked')
```

project **Browser**

project **MPC**

project **Service**

```
val b = input()  
send b to MPC(B..., S...)  
...  
output('leaked')
```

**Browser**

```
val b' = receive B...  
...
```

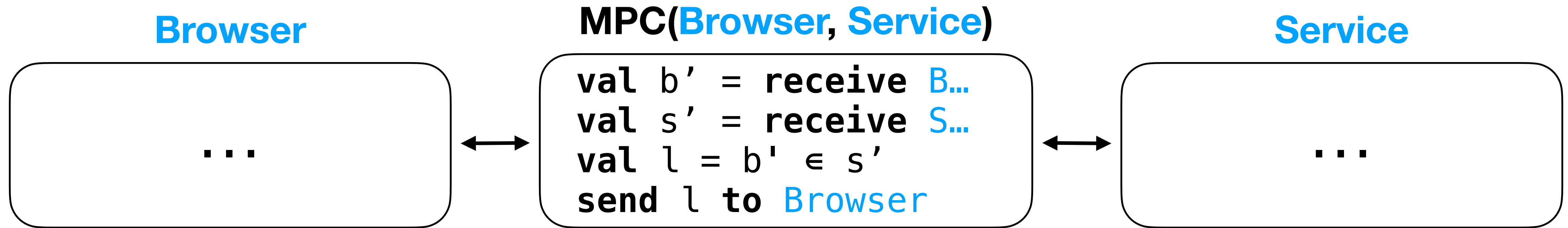
**MPC(Browser, Service)**

...

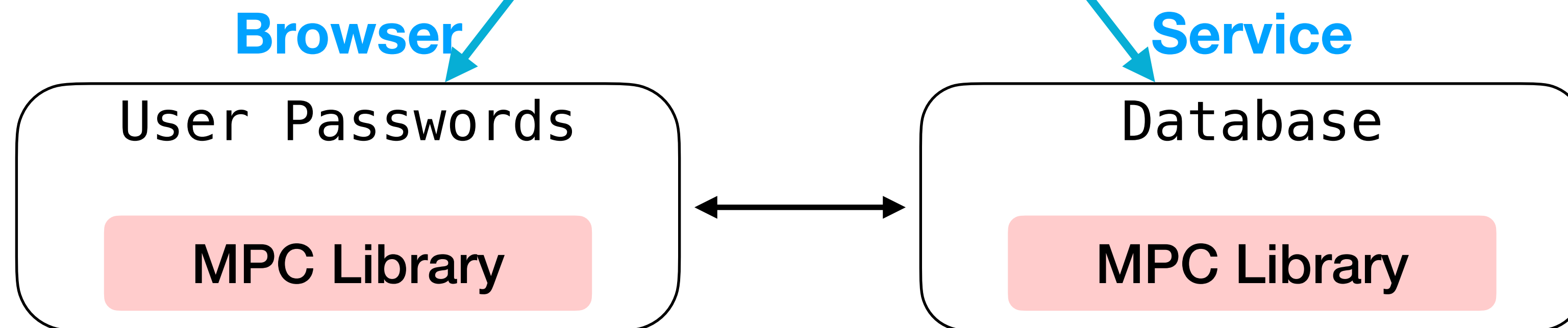
**Service**

# Cryptographic Instantiation

## IDEAL MODEL



## REAL IMPLEMENTATION



# Compilation Summary

Source Program

```
val x = e  
...
```

Choreography

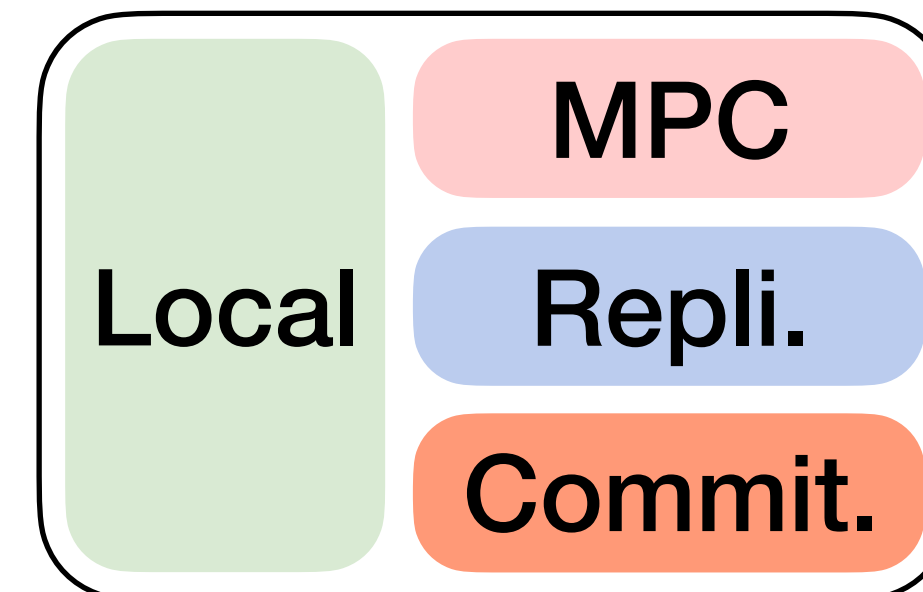
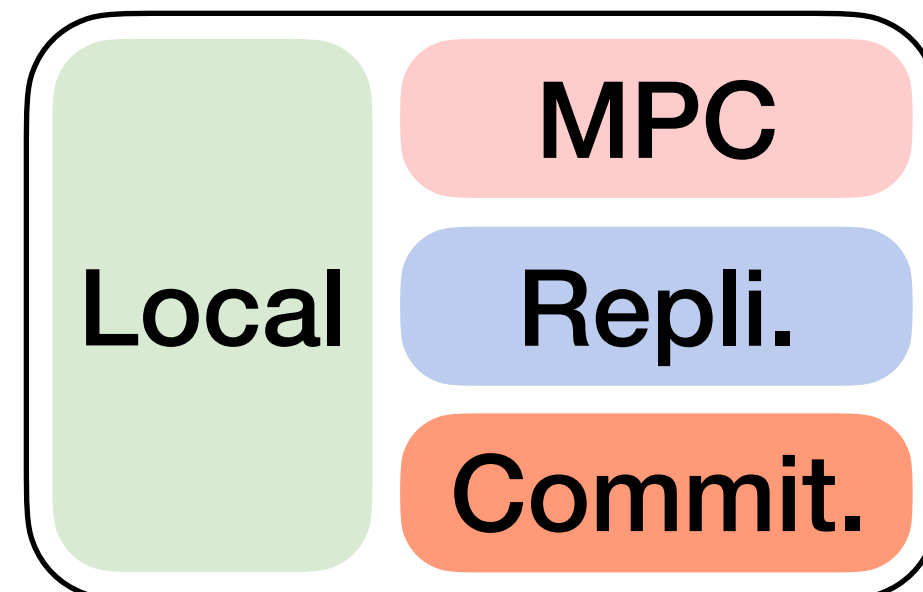
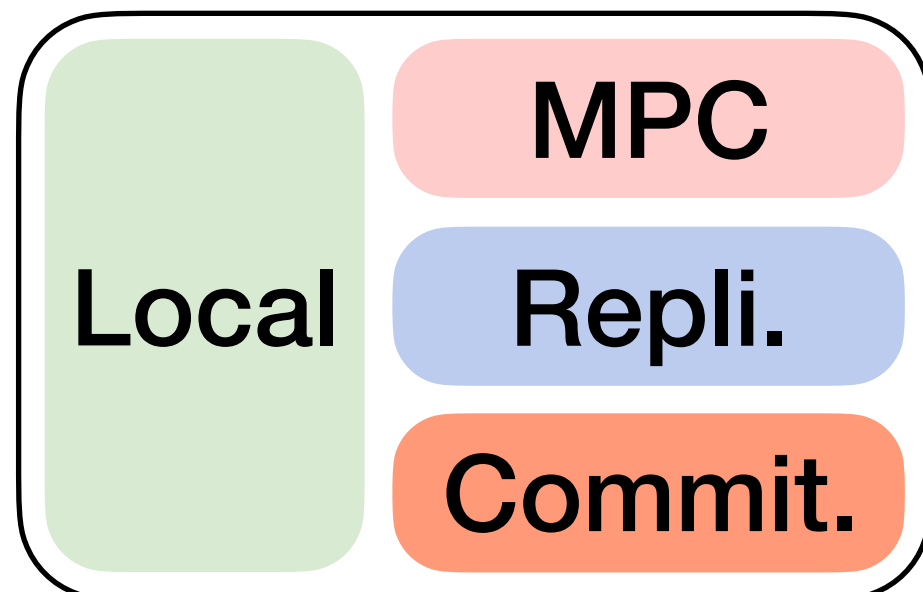
```
val x@Alice = e  
Alice.x ↗ MPC(A..., B...).y  
...
```



Alice

Bob

Chuck



Protocol Synthesis

Endpoint Projection

Instantiation

# Implementation & Scalability

- PLDI '21. Viaduct: An Extensible, Optimizing Compiler for Secure Distributed Programs.
  - Implements: Replication, Commitment, MPC via ABY, ZKP via libsnark
  - **Extensible**: can easily add more mechanisms
  - **Optimizing**: cost model + constrained optimization problem
  - **Expressive**: Label inference, label polymorphic functions
  - **Viable**: Evaluation and benchmarks



# Optimization Impact over Naive MPC

Benchmark	Protocols	Speedup over Naive MPC
HHI score	Local, MPC	67%
Biometric Match	Local, MPC	180%
Historical Millionaires	Local, MPC	100%
k-Means	MPC	150%
Median	Replication, MPC	1700%
Two-Round Bidding	Local, MPC	470%
Battleship	Replication, ZKP	—
Interval	ZKP, MPC	—

# Compiler Correctness

**Cryptography is notoriously *easy* to *get wrong*.**

**We must *prove* the correctness of Viaduct.**

# When is a Compiler Correct?

- Viaduct is only useful if developers can reason at the source level.

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- Viaduct is only useful if developers can reason at the source level.
- Many properties of interest:
  - **Functional correctness:** If Alice inputs 5 and Bob 7, the output is 12.
  - **Security:** Alice cannot infer  $x$ ; Bob cannot influence  $y$ .
  - **Corruption:** When Chuck is malicious...

# When is a Compiler Correct?

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- Many properties of interest:
  - **Functional correctness:** If Alice inputs 5 and Bob 7, the output is 12.
  - **Security:** Alice cannot infer  $x$ ; Bob cannot influence  $y$ .
  - **Corruption:** When Chuck is malicious...
- The compiler should preserve *all* properties!

# Robust Hyperproperty Preservation (RHP)

- Very strong compiler correctness criterion
  - Abate et al. (2019). *Journey Beyond Full Abstraction*. CSF
  - “Every hyperproperty source program has, the target has also.”
  - Hyperproperties: safety, liveness, noninterference, etc.
- RHP is the right notion of correctness for Viaduct

# Proof Requirements

1. **Property Preserving:** facilitates reasoning at source level
2. **Extensible:** does not fix set of cryptographic protocols
3. **Compositional:** interfaces with proofs of existing cryptography



# Universal Composability (UC)

- A framework for defining and proving security of cryptographic protocols
- Sequential and parallel composition maintains UC security
- UC simulation implies RHP
  - Patrignani et al. (2019). *Universal Composability is Secure Compilation*. CoRR
  - We independently verify UC implies RHP for our framework.

# Defining Security with Ideal Functionalities

Secure Channel (**Alice**, **Bob**)

```
val m = recv Alice
send len(m) to Adv
send m to Bob
```

# Defining Security with Ideal Functionalities

## Secure Channel (Alice, Bob)

```
val m = recv Alice
send len(m) to Adv
send m to Bob
```

### Alice

```
val x = Alice.input
send x to SC(A..., B...)
```

### Bob

```
val x = recv SC(A..., B...)
```

# Defining Security with Ideal Functionalities

“Obviously secure”

Secure Channel (**Alice**, **Bob**)

```
val m = recv Alice
send len(m) to Adv
send m to Bob
```

**Alice**

```
val x = Alice.input
send x to SC(A..., B...)
```

**Bob**

```
val x = recv SC(A..., B...)
```

# Defining Security with Ideal Functionalities

“Obviously secure”

Leaks length of message  
but nothing else

Secure Channel (**Alice**, **Bob**)

```
val m = recv Alice
send len(m) to Adv
send m to Bob
```

**Alice**

```
val x = Alice.input
send x to SC(A..., B...)
```

**Bob**

```
val x = recv SC(A..., B...)
```

# Defining Security with Ideal Functionalities

“Obviously secure”

Leaks length of message  
but nothing else

**Adversary** cannot change  
message

Secure Channel (**Alice**, **Bob**)

```
val m = recv Alice
send len(m) to Adv
send m to Bob
```

**Alice**

```
val x = Alice.input
send x to SC(A..., B...)
```

**Bob**

```
val x = recv SC(A..., B...)
```

# UC Simulation

REAL

Alice

Encryption

MAC

Insecure Network

Bob

Encryption

MAC

IDEAL

Secure Channel (Alice, Bob)

```
val m = recv Alice
send len(m) to Adv
send m to Bob
```

Alice

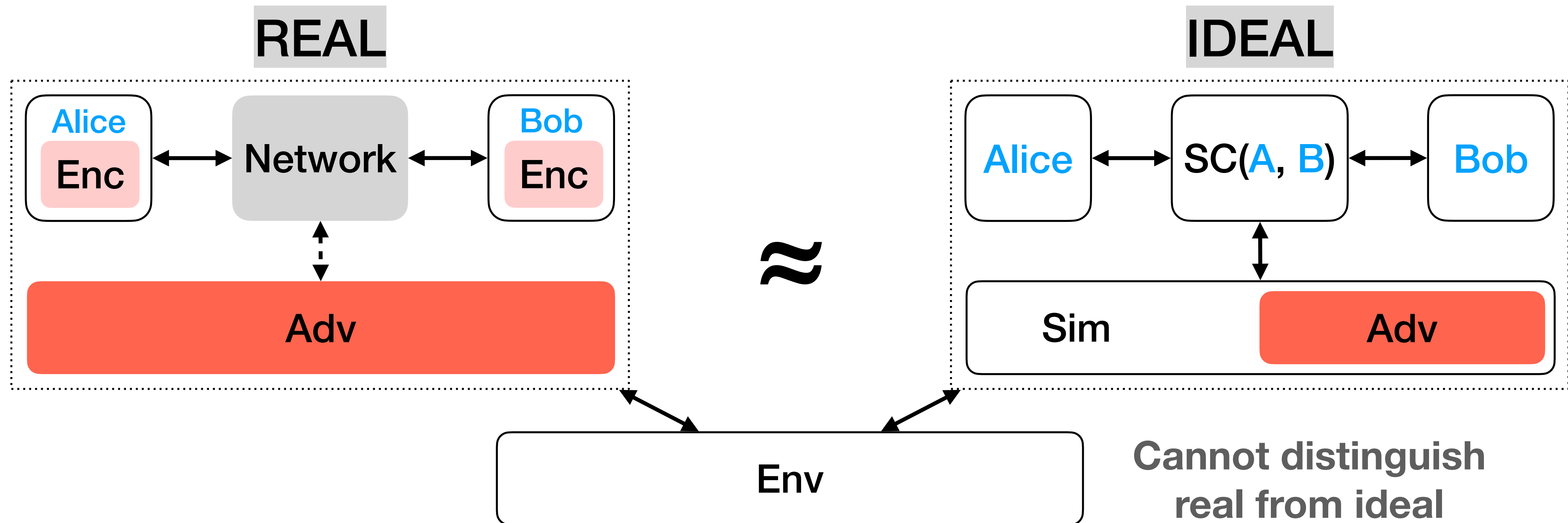
```
val x = Alice.input
send x to SC(A..., B...)
```

Bob

```
val x = recv SC(A..., B...)
```

$\Vdash$   
(simulates)

# UC Simulation



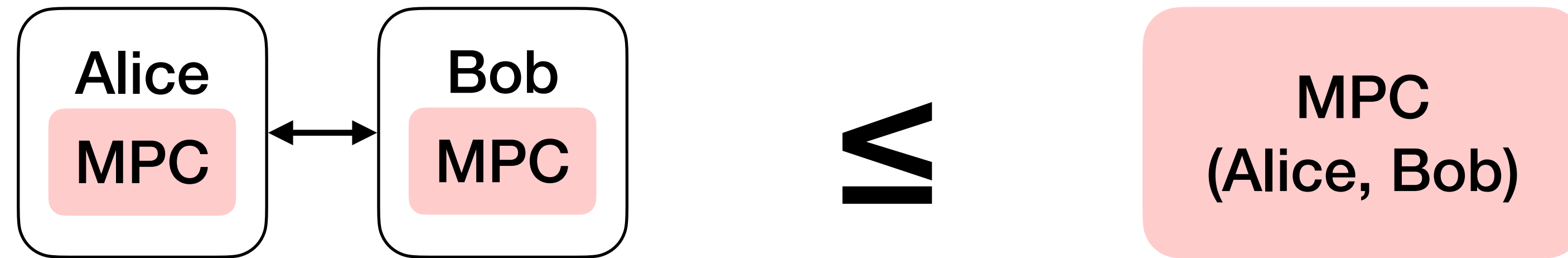
Every attack on the real system can be translated to an attack on the ideal system.



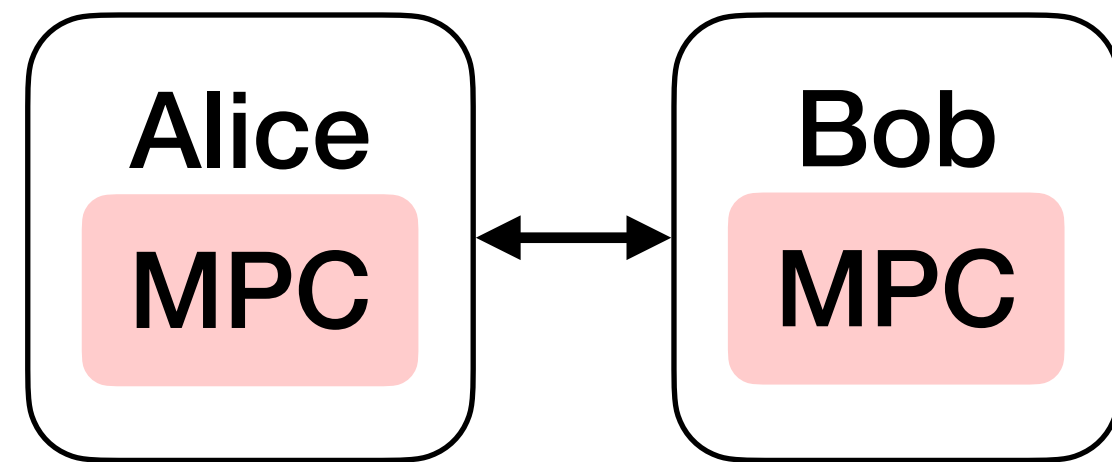
# UC Composition

**MPC**  
**(Alice, Bob)**

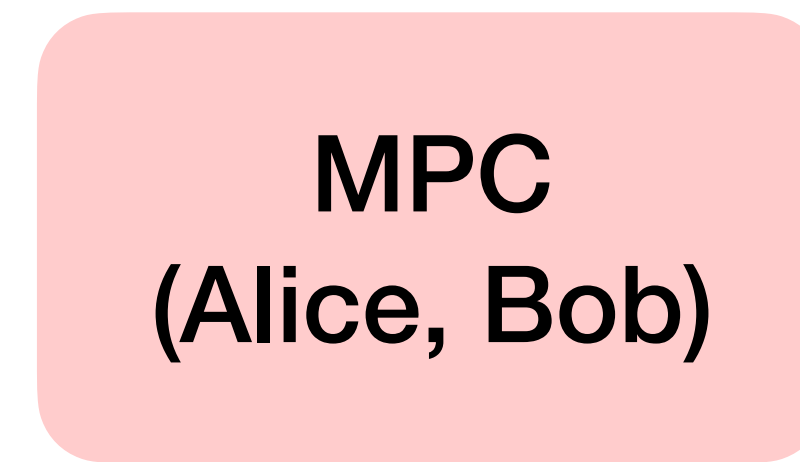
# UC Composition



# UC Composition

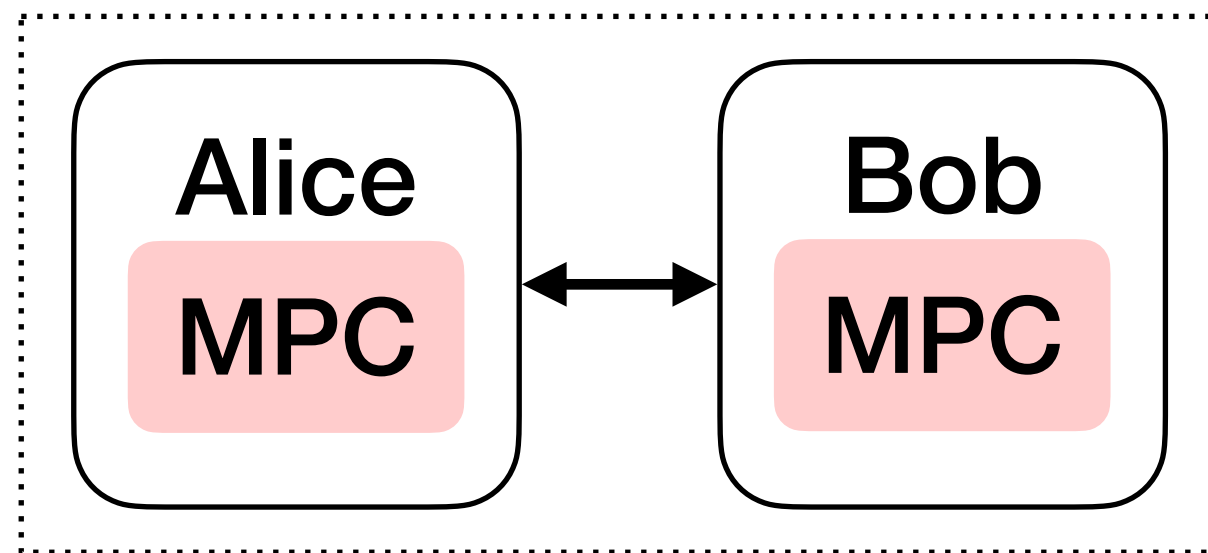


$\equiv$

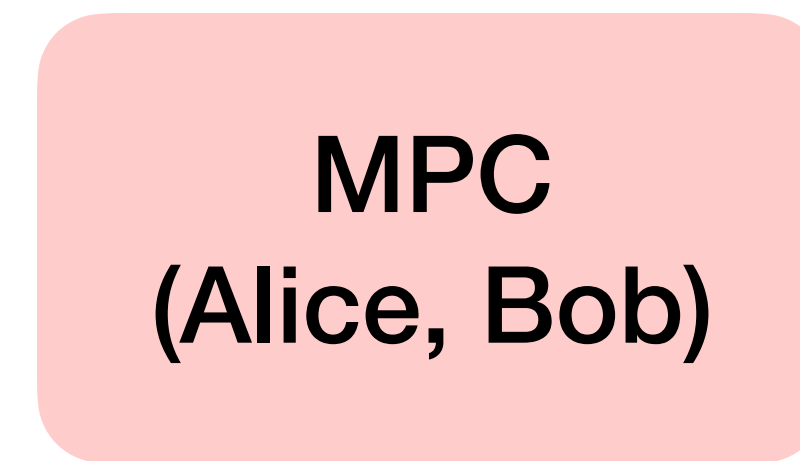


THEN

Subprotocol



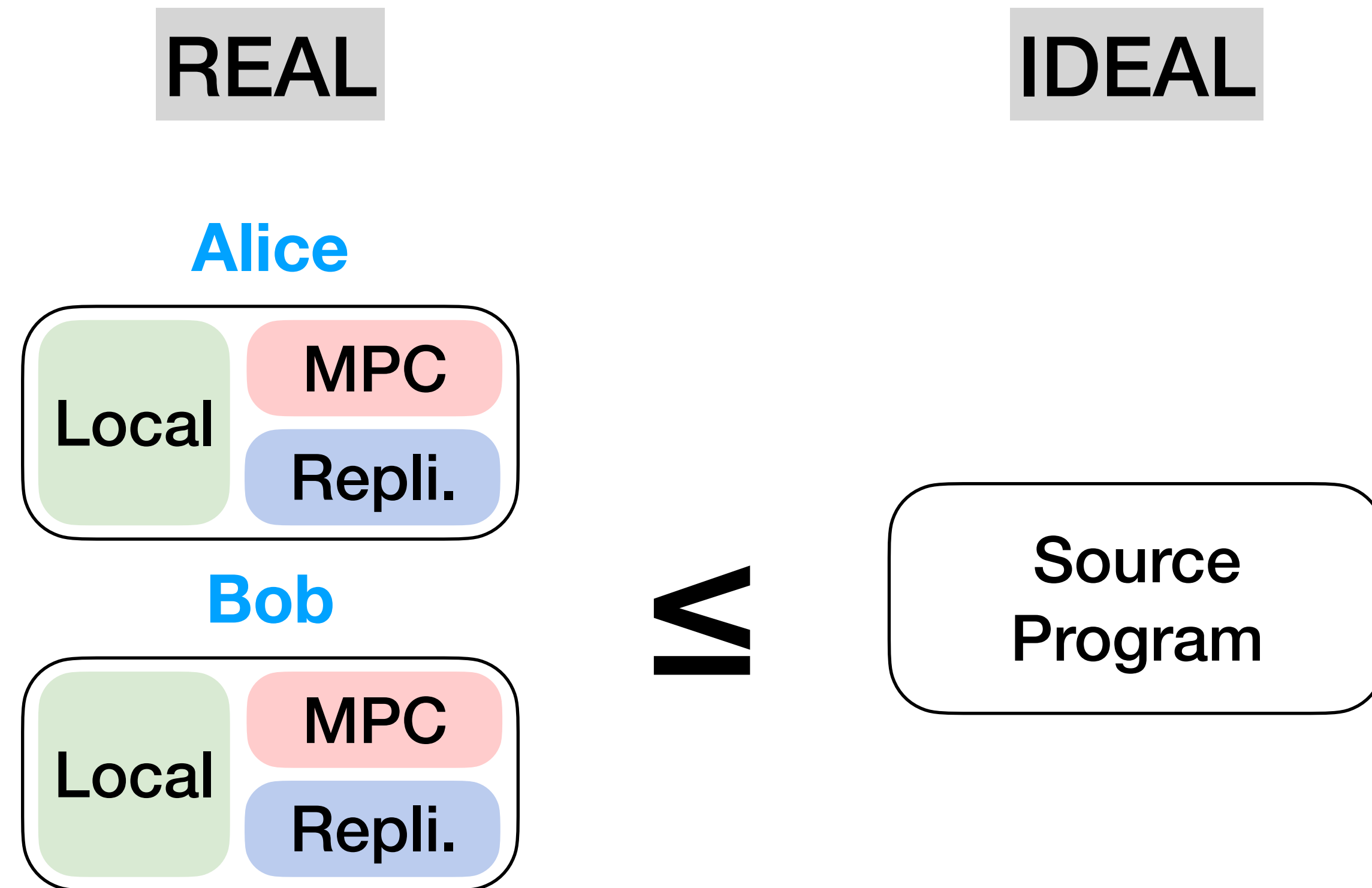
$\equiv$



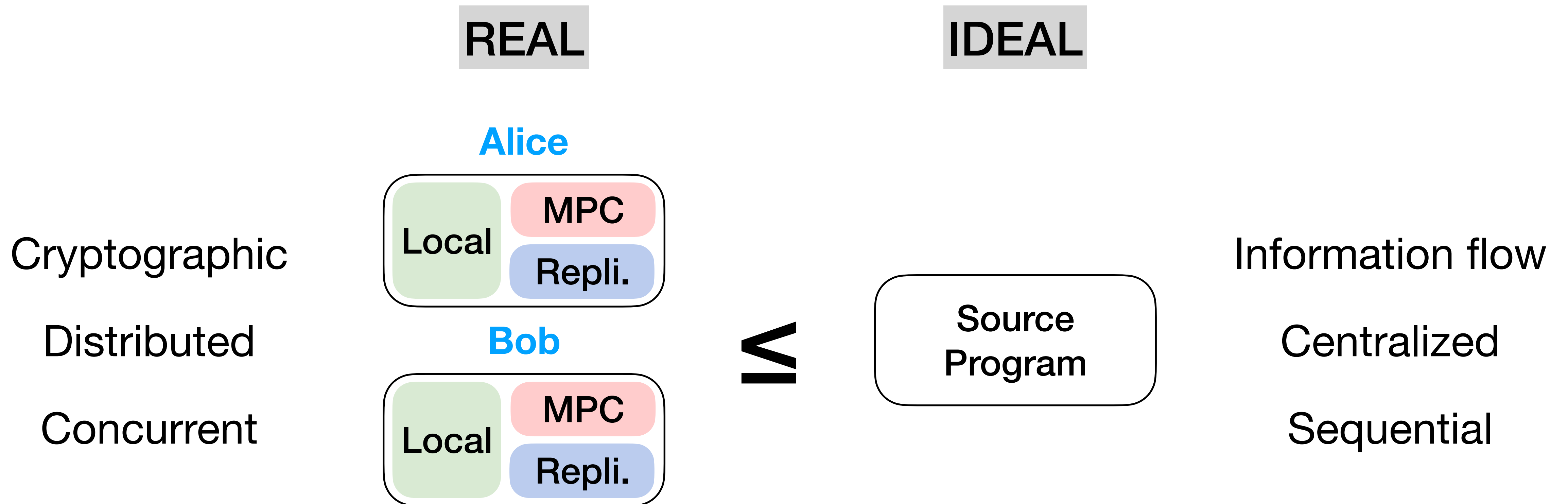
# Structure of a UC Proof

- Formally, UC states:
  - $\forall \text{Adv} \exists \text{Sim} \forall \text{Env} \cdot \text{Adv} \parallel \text{Real} \sim_{\text{Env}} \text{Sim} \parallel \text{Ideal}$
- To prove UC simulation:
  - Define real protocol and ideal functionality
  - Construct a **Simulator** given an arbitrary **Adversary**
  - Come up with invariant maintained throughout execution
  - Show invariant implies bisimulation from perspective of Environment

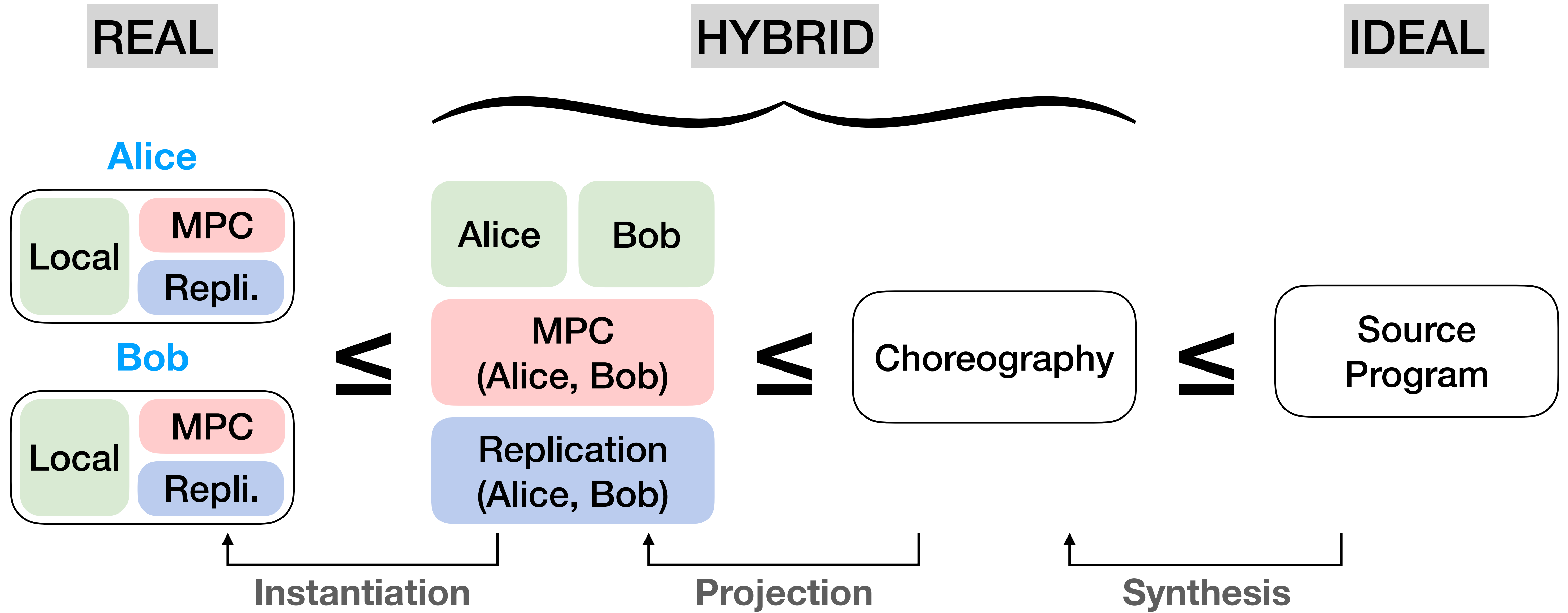
# Show Compiled Code Simulates Source



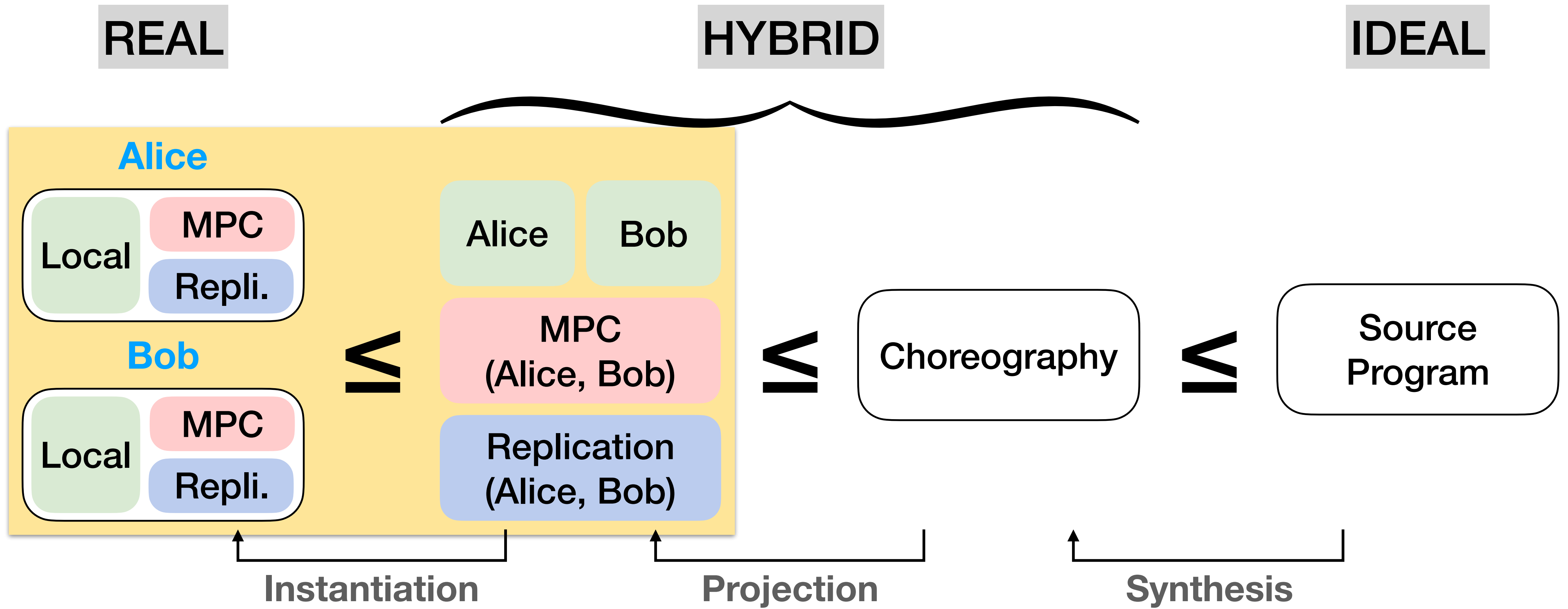
# Show Compiled Code Simulates Source



# UC Simulation is Transitive



# Correctness of Cryptographic Instantiation

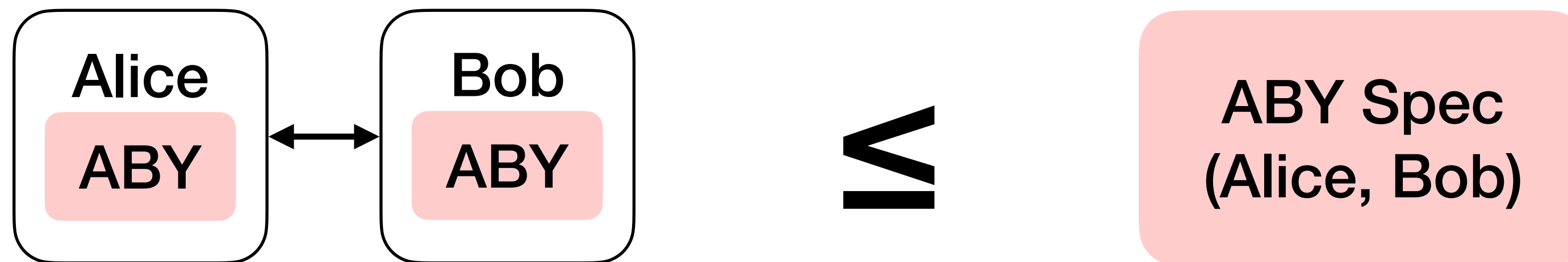




# Appeal to Existing UC Proofs

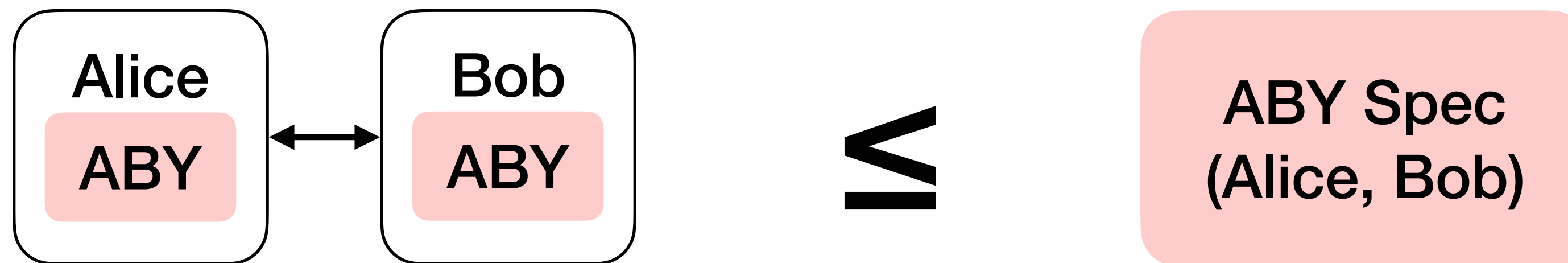
# Appeal to Existing UC Proofs

- Take an existing library and proof of correctness

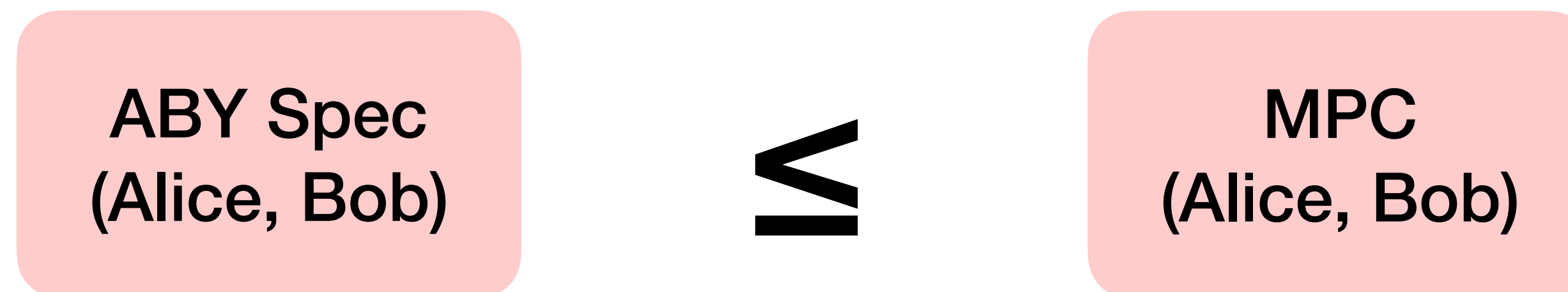


# Appeal to Existing UC Proofs

- Take an existing library and proof of correctness



- Verify library interface matches our ideal functionality



# Appeal to Existing UC Proofs

- Apply repeatedly for each ideal host
- Uses transitivity and UC composition

# Appeal to Existing UC Proofs

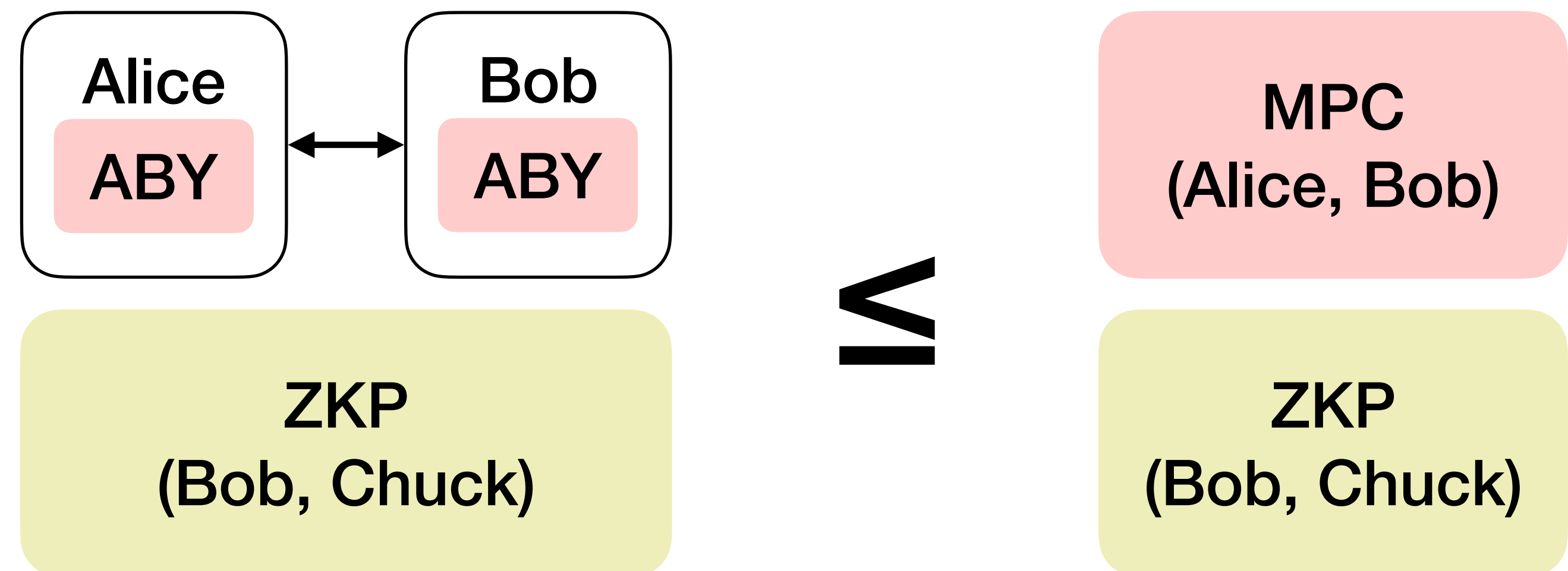
- Apply repeatedly for each ideal host
- Uses transitivity and UC composition

**MPC**  
(Alice, Bob)

**ZKP**  
(Bob, Chuck)

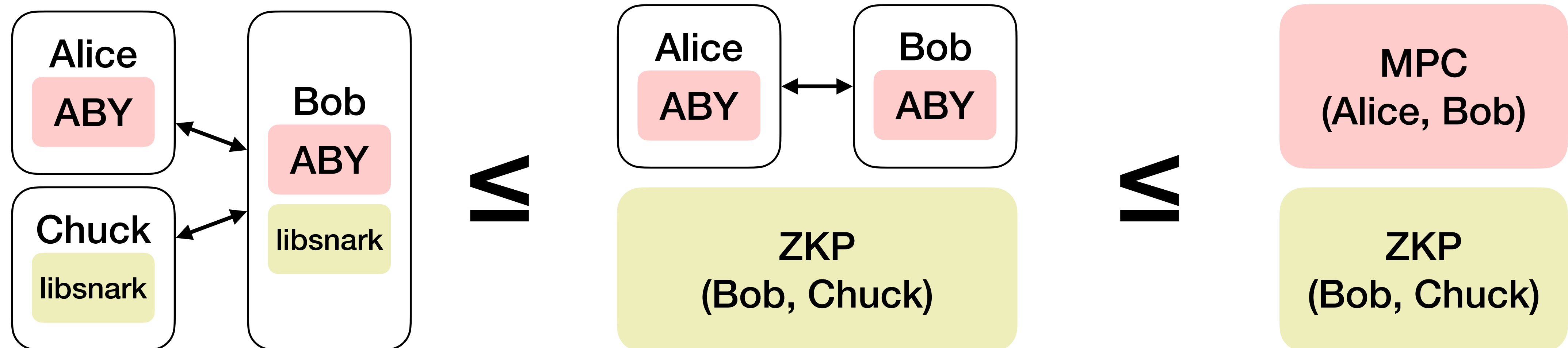
# Appeal to Existing UC Proofs

- Apply repeatedly for each ideal host
- Uses transitivity and UC composition

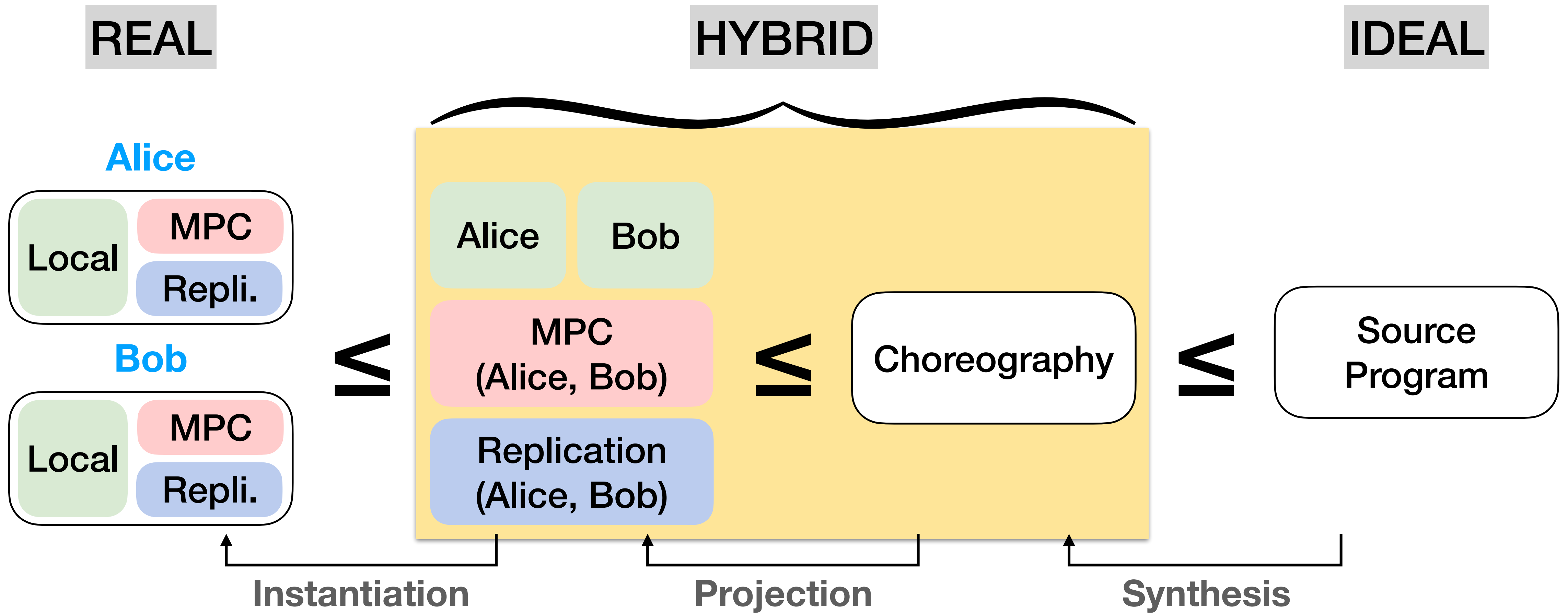


# Appeal to Existing UC Proofs

- Apply repeatedly for each ideal host
- Uses transitivity and UC composition



# Correctness of Endpoint Projection





# Appeal to Choreography Literature

- This is exactly what choreography literature tries to prove
  - “Soundness and completeness of endpoint projection”
  - Luís Cruz-Filipe et al. (2022). *A Formal Theory of Choreographic Programming*. CoRR
- Choreographies are alternative representations of distributed systems
- But they have the same exact behavior (i.e., traces)

# Choreographies are Concurrent

Alice

```
val x = input
```

Bob

```
output(2)
```

$\cong$

Choreography

```
val x@Alice = input  
Bob.output(2)
```

# Choreographies are Concurrent

Alice

```
val x = input
```

Bob

```
output(2)
```

Adversary can step  
Bob before Alice

$\not\equiv$

Choreography

```
val x@Alice = input  
Bob.output(2)
```

# Choreographies are Concurrent

Alice

```
val x = input
```

Bob

```
output(2)
```

Adversary can step  
Bob before Alice

$\cong$

Choreography

```
val x@Alice = input  
Bob.output(2)
```

Simulator can step  
Bob before Alice

# Choreographies Model Communication

Alice

```
val x = input  
send x to Bob
```

Bob

```
val y = receive Alice
```

$\Vdash$

Choreography

```
val x@Alice = input  
Alice.x  $\rightsquigarrow$  Bob.y
```

# Choreographies Model Communication

Alice

```
val x = input  
send x to Bob
```

Bob

```
val y = receive Alice
```

$\equiv$

Choreography

```
val x@Alice = input  
Alice.x  $\rightsquigarrow$  Bob.y
```

Generates message  
readable by **Adversary**

# Choreographies Model Communication

Alice

```
val x = input  
send x to Bob
```

Bob

```
val y = receive Alice
```

Generates message  
readable by **Adversary**

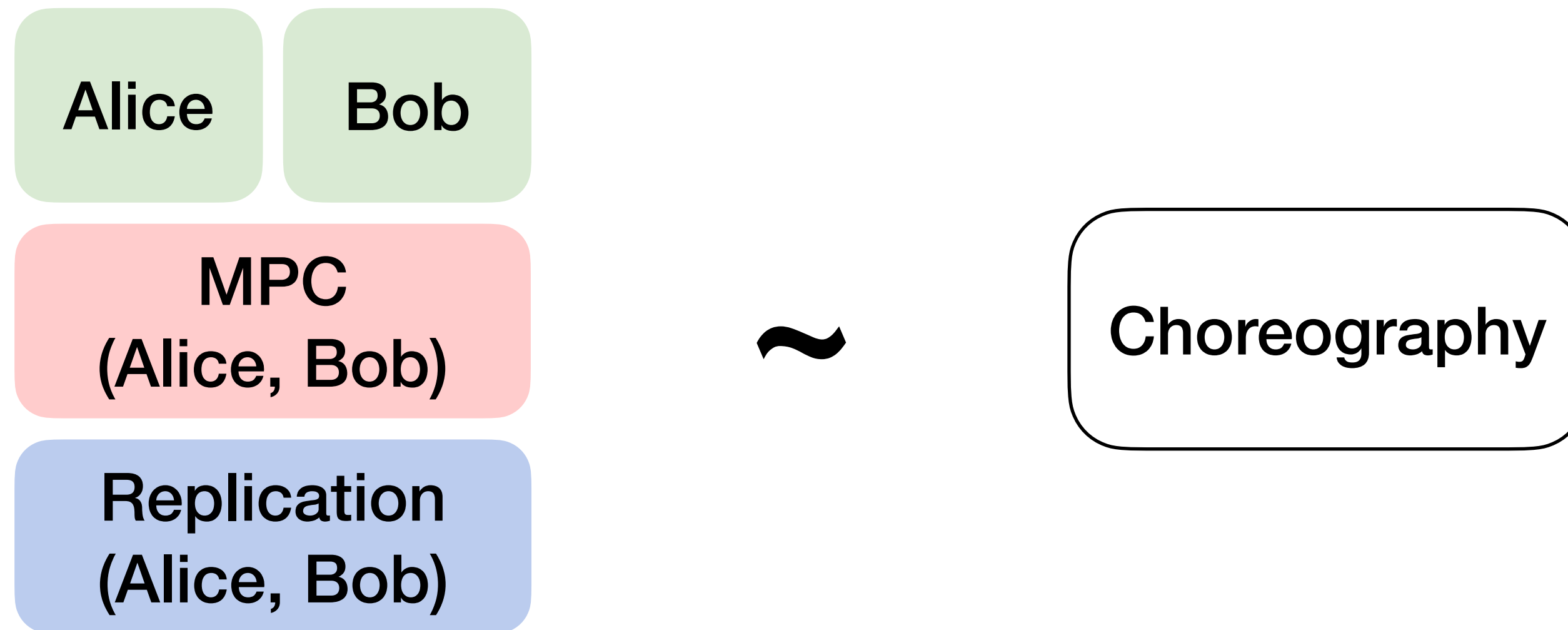
$\Vdash$

Choreography

```
val x@Alice = input  
Alice.x  $\rightsquigarrow$  Bob.y
```

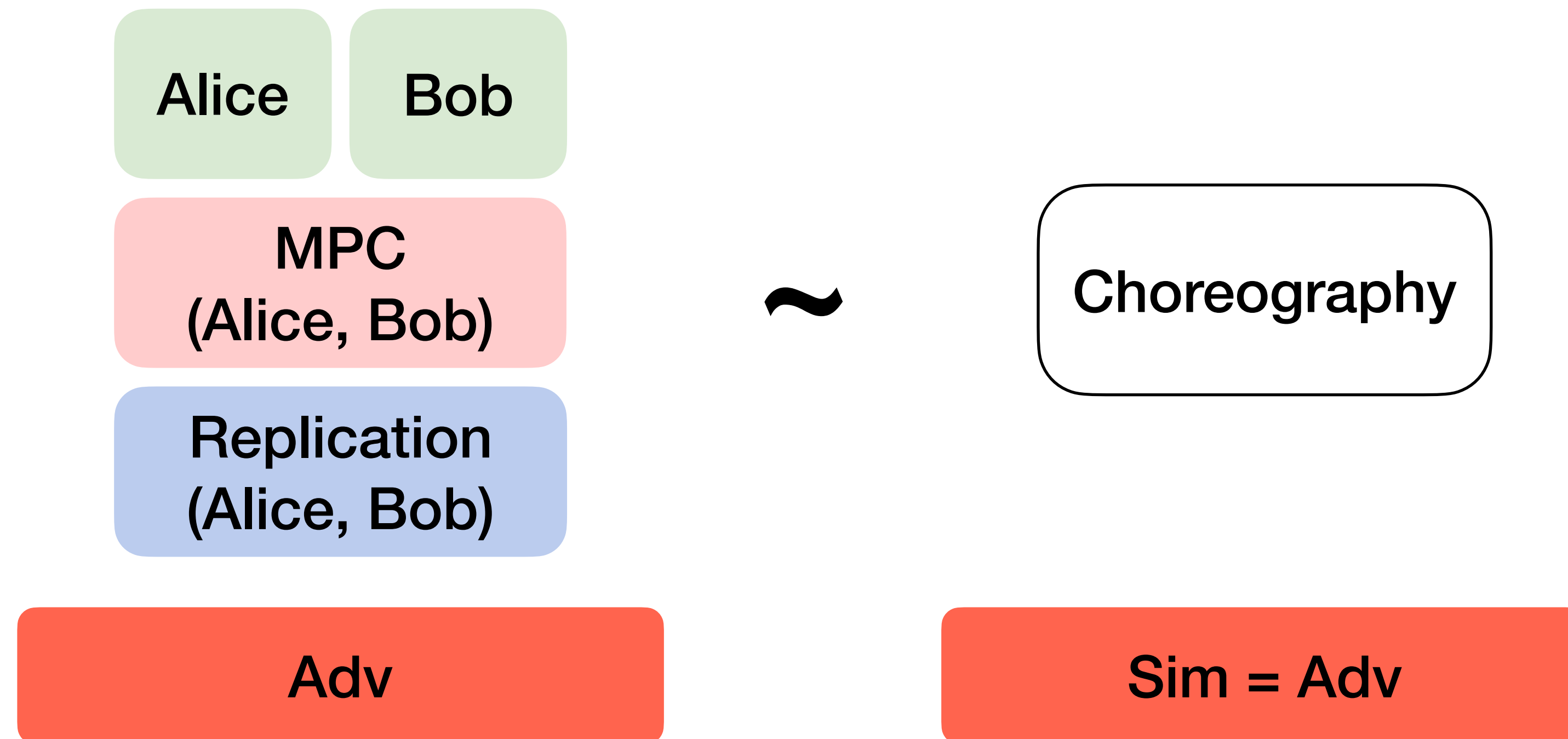
Generates message  
readable by **Simulator**

# Choreographies and Projection are Bisimilar

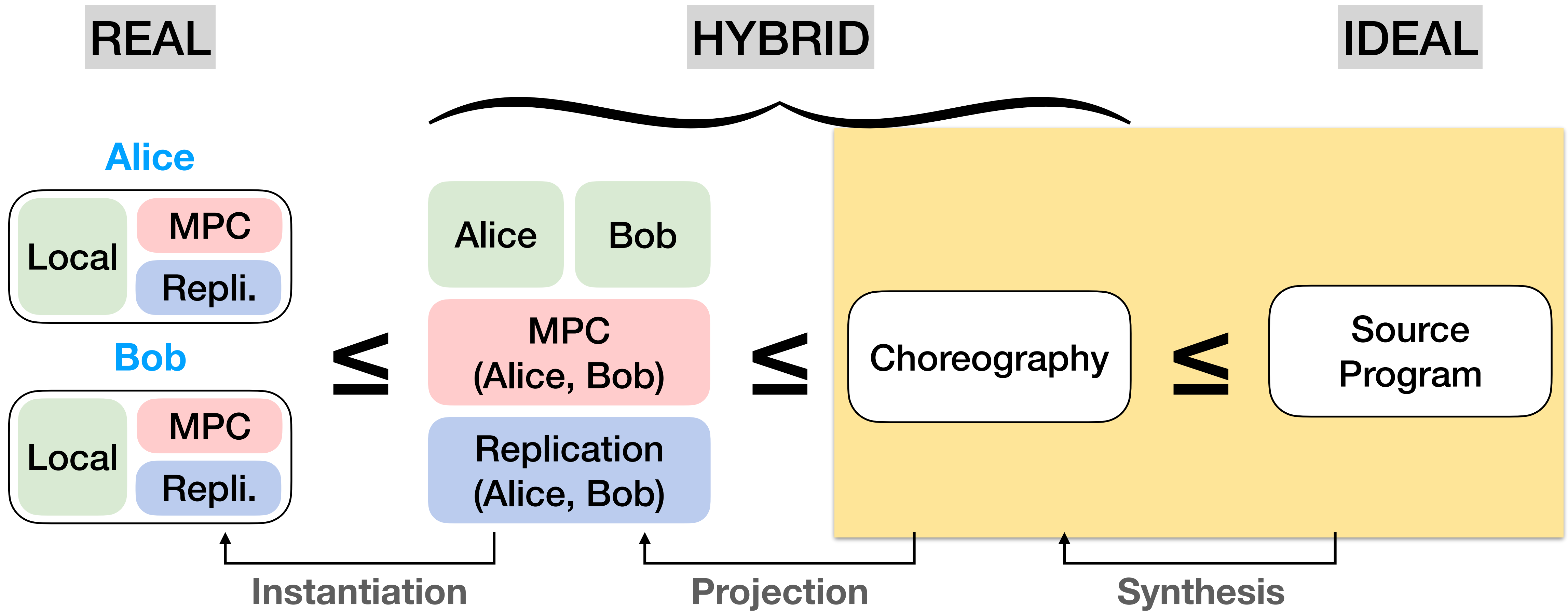




# Choreographies and Projection are Bisimilar



# Correctness of Protocol Synthesis



# Comparing Choreography to Source

## Choreography

```
val x@Alice = e  
Bob.output(2)  
Alice.x ↗ Bob.y
```

≅

## Source Program

```
val x = e  
Bob.output(2)
```

# Comparing Choreography to Source

## Choreography

```
val x@Alice = e  
Bob.output(2)  
Alice.x ↗ Bob.y
```

≅

## Source Program

```
val x = e  
Bob.output(2)
```

- Similar:
  - Abstract away cryptography
  - Centralized

# Comparing Choreography to Source

## Choreography

```
val x@Alice = e  
Bob.output(2)  
Alice.x ↗ Bob.y
```

≅

## Source Program

```
val x = e  
Bob.output(2)
```

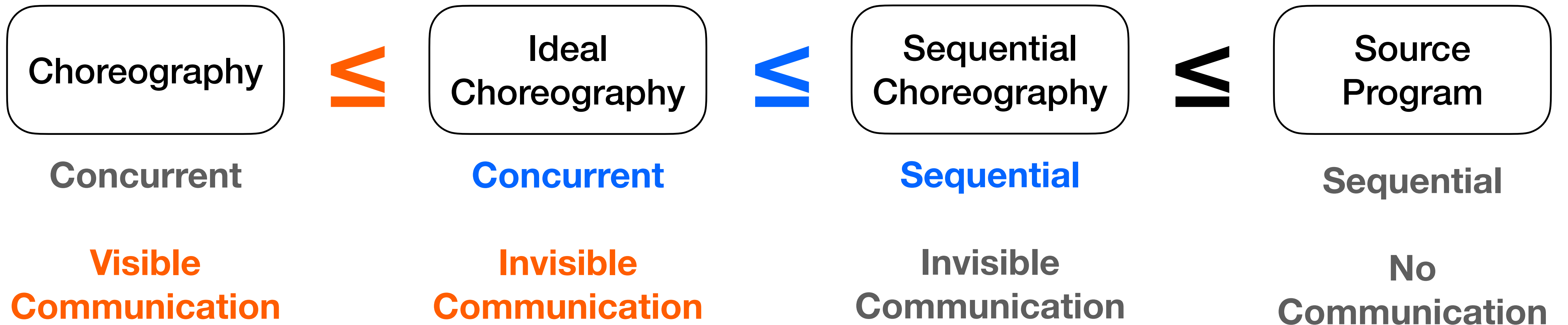
- Similar:

- Abstract away cryptography
- Centralized

- Different:

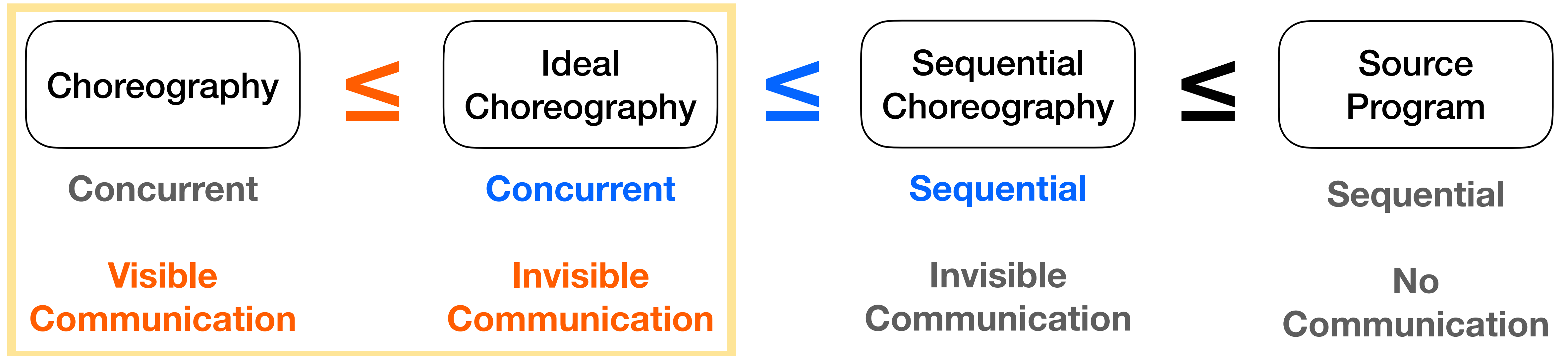
1. Locations & explicit communication
2. Concurrency

# Break Up Proof Using Transitivity



Define intermediate languages with altered semantics.

# Correctness of Idealization



# Explicit Communication: Confidentiality

## Choreography

```
val x@Alice = input  
Alice.x ↗ Bob.y
```

≅

## Source Program


```
val x = Alice.input
```



# Explicit Communication: Confidentiality

## Choreography

```
val x@Alice = input  
Alice.x ↗ Bob.y
```



≅

## Source Program

```
val x = Alice.input
```

- Generates event in trace
- If **Bob** is corrupted:
  - x is leaked to **Adversary**

# Explicit Communication: Confidentiality

## Choreography

```
val x@Alice = input  
Alice.x ↗ Bob.y
```

≡

## Source Program

```
val x = Alice.input
```

- Generates event in trace
- If **Bob** is corrupted:
  - x is leaked to **Adversary**

# Explicit Communication: Confidentiality

## Choreography

```
val x@Alice = input
Alice.x ↔ Bob.y
```

~~≡~~

## Source Program

```
val x = Alice.input
```

- Generates event in trace
- If **Bob** is corrupted:
  - x is leaked to **Adversary**

# Explicit Communication: Integrity

## Choreography

```
val x@Alice = 1  
Alice.x ↗ Bob.x'  
Bob.output(x')
```



## Source Program

```
val x = 1  
Bob.output(x)
```

# Explicit Communication: Integrity

## Choreography

```
val x@Alice = 42  
Alice.x ↗ Bob.x'  
Bob.output(x')
```



## Source Program

```
val x = 1  
Bob.output(x)
```

ALICE CORRUPTED

# Explicit Communication: Integrity

## Choreography

```
val x@Alice = 42  
Alice.x ↗ Bob.x'  
Bob.output(x')
```



## Source Program

```
val x = 1  
Bob.output(x)
```

ALICE CORRUPTED

- If **Alice** is corrupted:
  - **Adversary** controls  $x'$

# Explicit Communication: Integrity

## Choreography

```
val x@Alice = 42  
Alice.x ↗ Bob.x'  
Bob.output(x')
```

~~≡~~

## Source Program

```
val x = 1  
Bob.output(x)
```

ALICE CORRUPTED

Always outputs 1

- If **Alice** is corrupted:
  - **Adversary** controls  $x'$

# Information Flow Typing to the Rescue

- Define information flow type system for *choreographies*
- *Require* protocol synthesis to output well-typed choreographies

## Confidentiality Violation

```
val x@Alice = input
Alice.x ↗ Bob.y
```

Alice doesn't trust Bob  
with confidentiality

## Integrity Violation

```
val x@Alice = 1
Alice.x ↗ Bob.x'
Bob.output(x')
```

Bob doesn't trust Alice  
with integrity



# Downgrades Relax Security Policy

- Use **declassify/endorse** to specify intended policy:

## Allow Send to Bob

```
val x@Alice = input
val x' = decl(x, Bob)
Alice.x' ↗ Bob.y
```

## Allow Receive from Alice

```
val x@Alice = 1
Alice.x ↗ Bob.x'
val x'' = end(x, Bob)
Bob.output(x'')
```

# Downgrades as Adversarial Interaction

# Downgrades as Adversarial Interaction

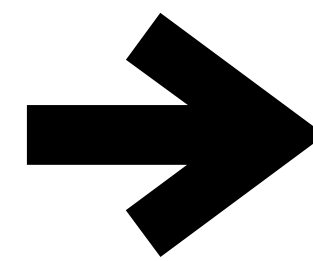
- We model downgrades as communication with the **Adversary**
  - **declassify**(x, **Host**): send x to **Adversary** (if **Host** is public)
  - **endorse**(x, **Host**): receive x from **Adversary** (if x is untrusted)

# Downgrades as Adversarial Interaction

- We model downgrades as communication with the **Adversary**
  - **declassify**(x, **Host**): send x to **Adversary** (if **Host** is public)
  - **endorse**(x, **Host**): receive x from **Adversary** (if x is untrusted)
- Commonplace in UC:

Secure Channel (**Alice**, **Bob**)

```
val m = recv Alice
send len(m) to Adv
send m to Bob
```



Secure Channel (**Alice**, **Bob**)

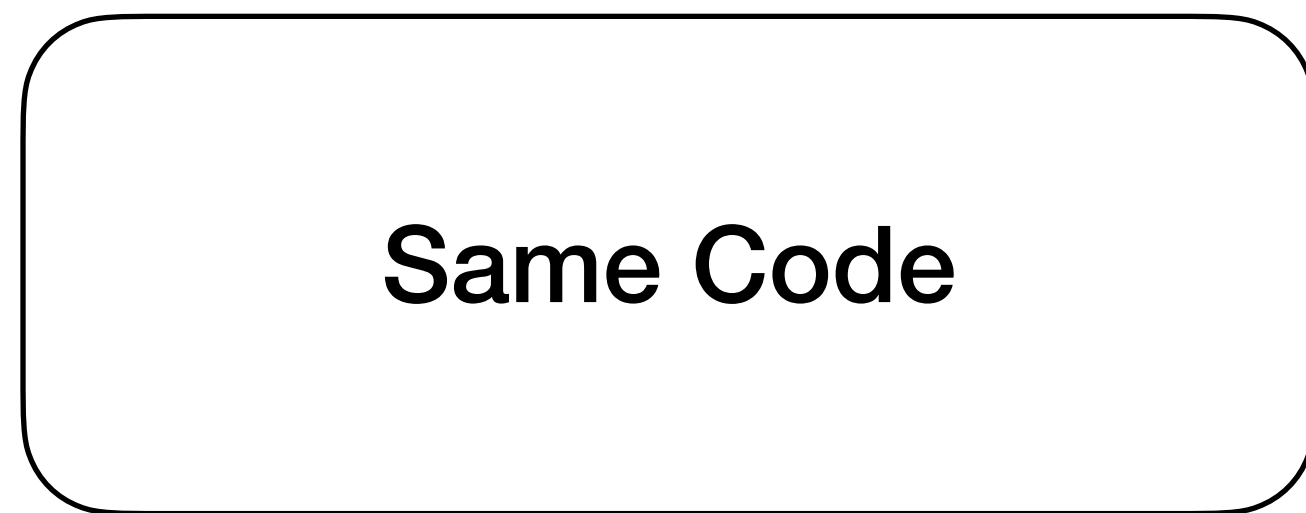
```
val m = recv Alice
declassify(len(m))
send m to Bob
```

# Verifying the Type System

- Type system ensures
  - Secret data is not sent to public hosts
  - Untrusted data does not influence trusted hosts
- How do we know?

# Ideal Choreographies

## Choreography



≡

## Ideal Choreography



Communication generates  
external events

Untrusted hosts produce  
arbitrary data

**declassify/endorse** internal

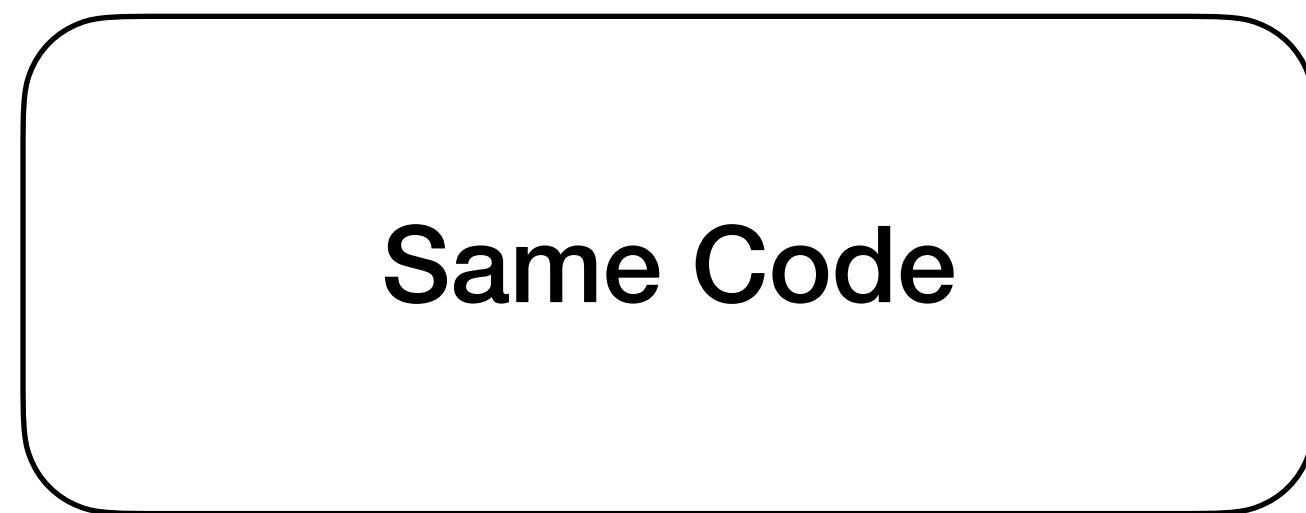
Communication generates  
internal events

Untrusted data replaced with  
dummy value (i.e., 0)

**declassify/endorse** external

# Ideal Choreographies

**Choreography**



**≅**

**Ideal Choreography**



Communication generates  
external events

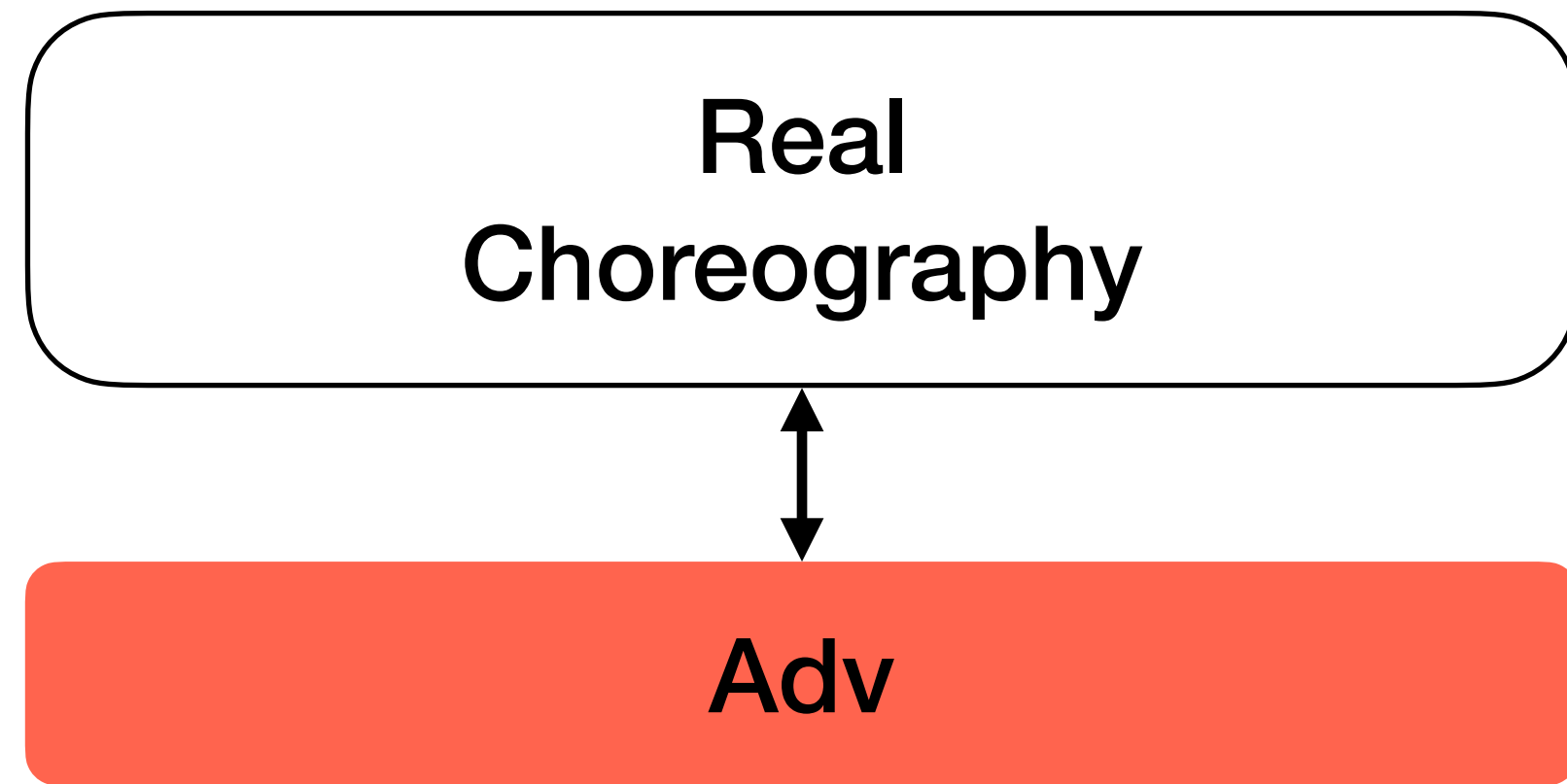
Communication generates  
internal events

**All corruption localized to declassify/endorse.**

**declassify/endorse** internal

**declassify/endorse** external

# Real Simulates Ideal

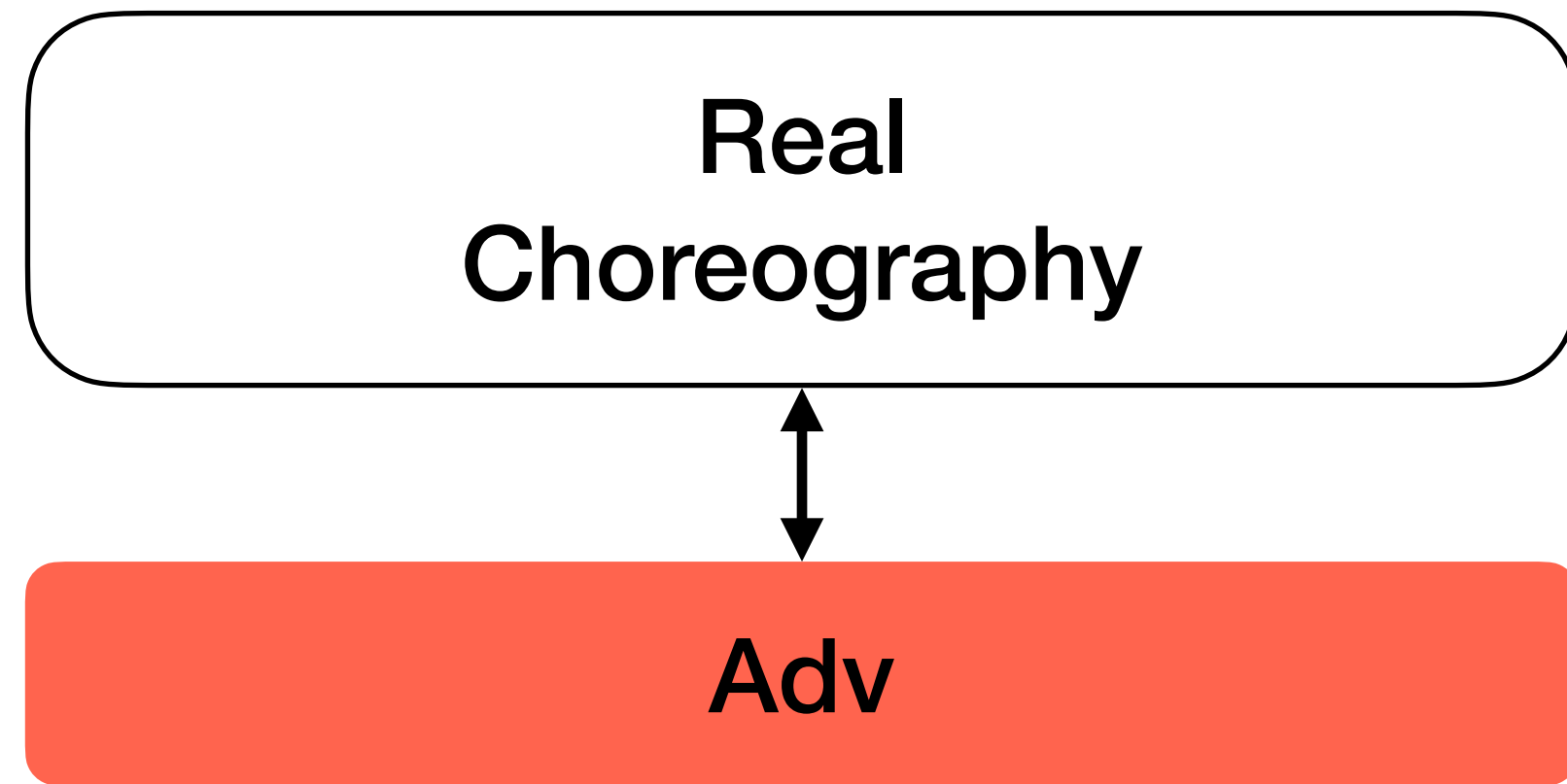


**VI**

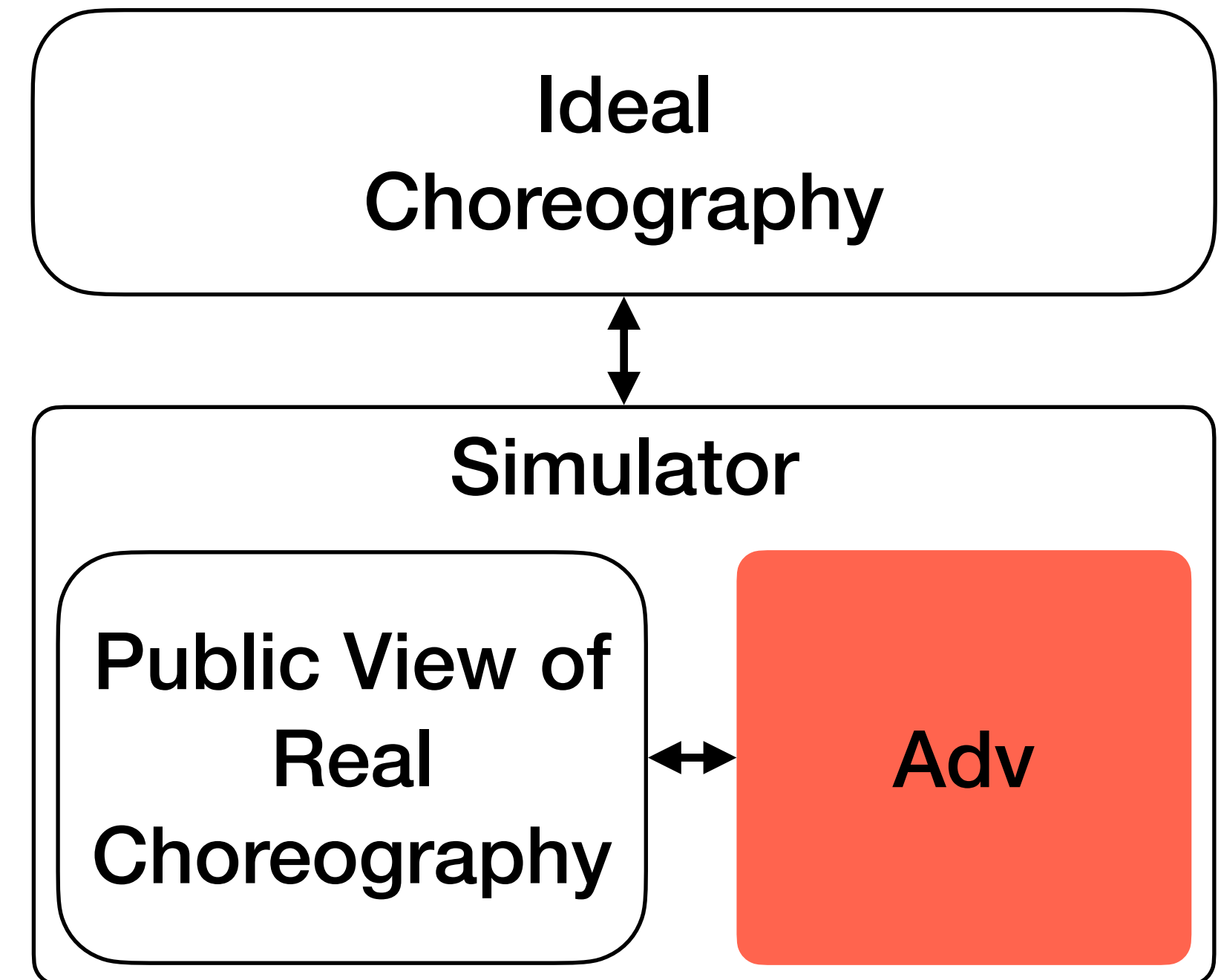




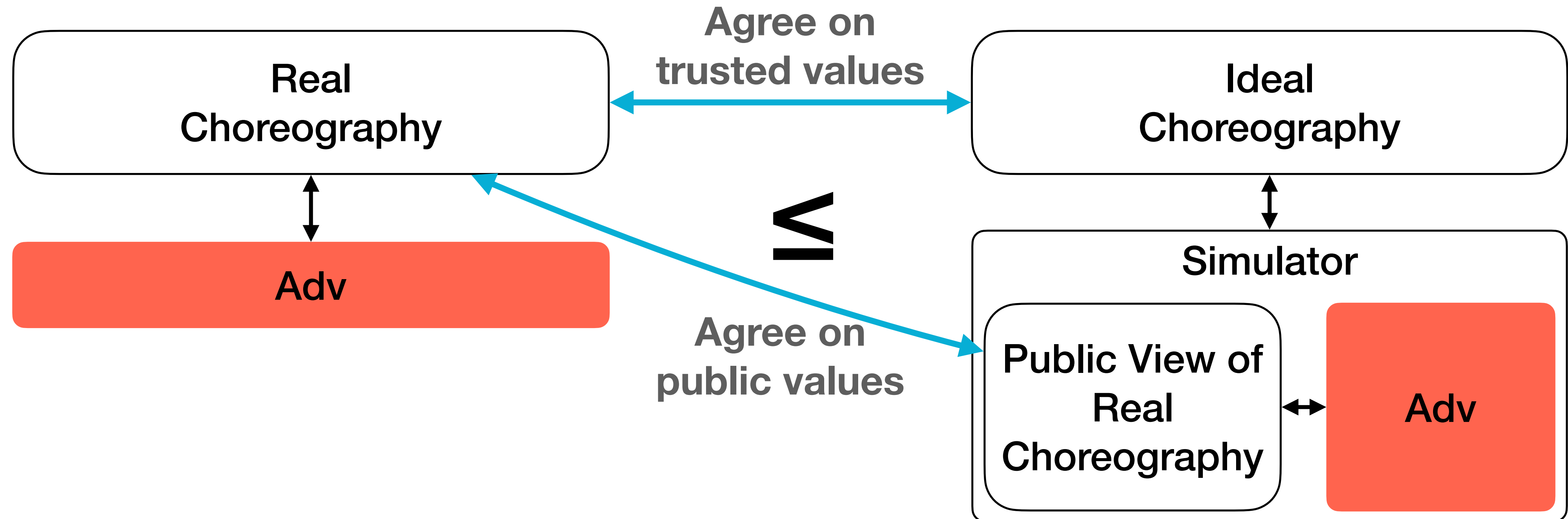
# Real Simulates Ideal



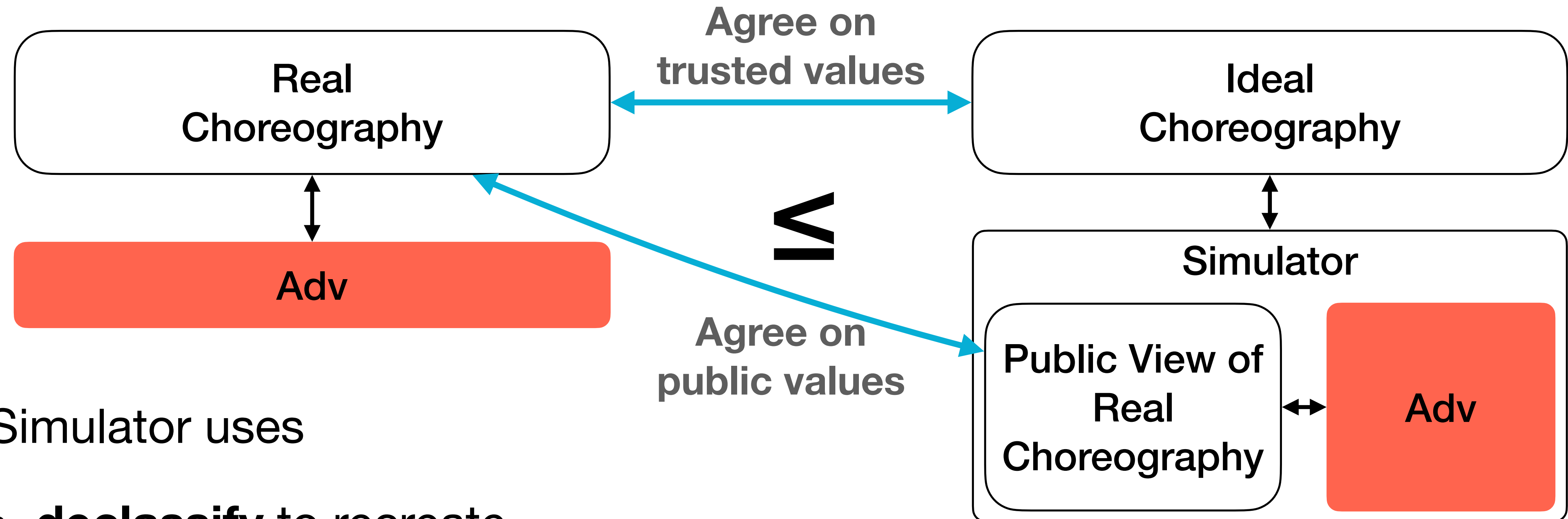
**VI**



# Real Simulates Ideal



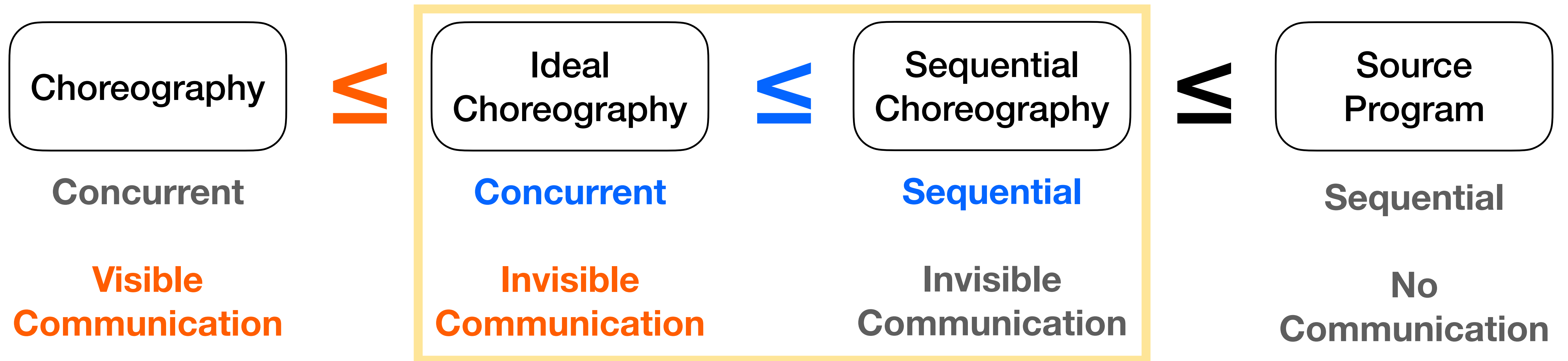
# Real Simulates Ideal



Simulator uses

- **declassify** to recreate messages no longer leaked
- **endorse** to corrupt data no longer corruptible

# Correctness of Sequentialization



# Unrestricted Concurrency Violates Security

## Source Program

```
val g' = endorse(guess, C)  
val s' = decl(secret, C)
```

I picked a secret number.  
You guess, *then* I reveal.

# Unrestricted Concurrency Violates Security

## Insecure Choreography

```
val g'@S1 = endorse(guess, C)  
val s'@S2 = decl(secret, C)
```



## Source Program

```
val g' = endorse(guess, C)  
val s' = decl(secret, C)
```

I picked a secret number.  
You guess, *then* I reveal.

This choreography can  
reorder these events!

# Require Synchronization

- A novel type system for *choreographies* that checks synchronization
- *Require* protocol synthesis to output well-synchronized choreographies
- Requires minimal synchronization
  - Outputs (**declassify**) must be ordered wrt. prior inputs (**endorse**)
  - We do not order internal events, inputs wrt. inputs etc.

# Require Synchronization

- A novel type system for *choreographies* that checks synchronization
- *Require* protocol synthesis to output well-synchronized choreographies
- Requires minimal synchronization
  - Outputs (**declassify**) must be ordered wrt. prior inputs (**endorse**)
  - We do not order internal events, inputs wrt. inputs etc.

## Insecure Choreography

```
val g'@S1 = endorse(guess, C)
val s'@S2 = decl(secret, C)
```

## Secure Choreography

```
val g'@S1 = endorse(guess, C)
S1.0 ↗ S2._
val s'@S2 = decl(secret, C)
```



# Ideal Simulates Sequential

## Sequential Choreography

```
val x = S2.input()  
val g' = endorse(guess, C)  
S1.0 ↗ S2._  
val s' = decl(secret, C)
```

≧

May evaluate: g', x, s'

Must evaluate: x, g', s'

# Ideal Simulates Sequential

## Concurrent Choreography

```
val x = S2.input()
val g'@S1 = endorse(guess, C)
S1.0 ↗ S2._
val s'@S2 = decl(secret, C)
```

May evaluate: g', x, s'

≧

## Sequential Choreography

```
val x = S2.input()
val g' = endorse(guess, C)
S1.0 ↗ S2._
val s' = decl(secret, C)
```

Must evaluate: x, g', s'

# Ideal Simulates Sequential

# Ideal Simulates Sequential

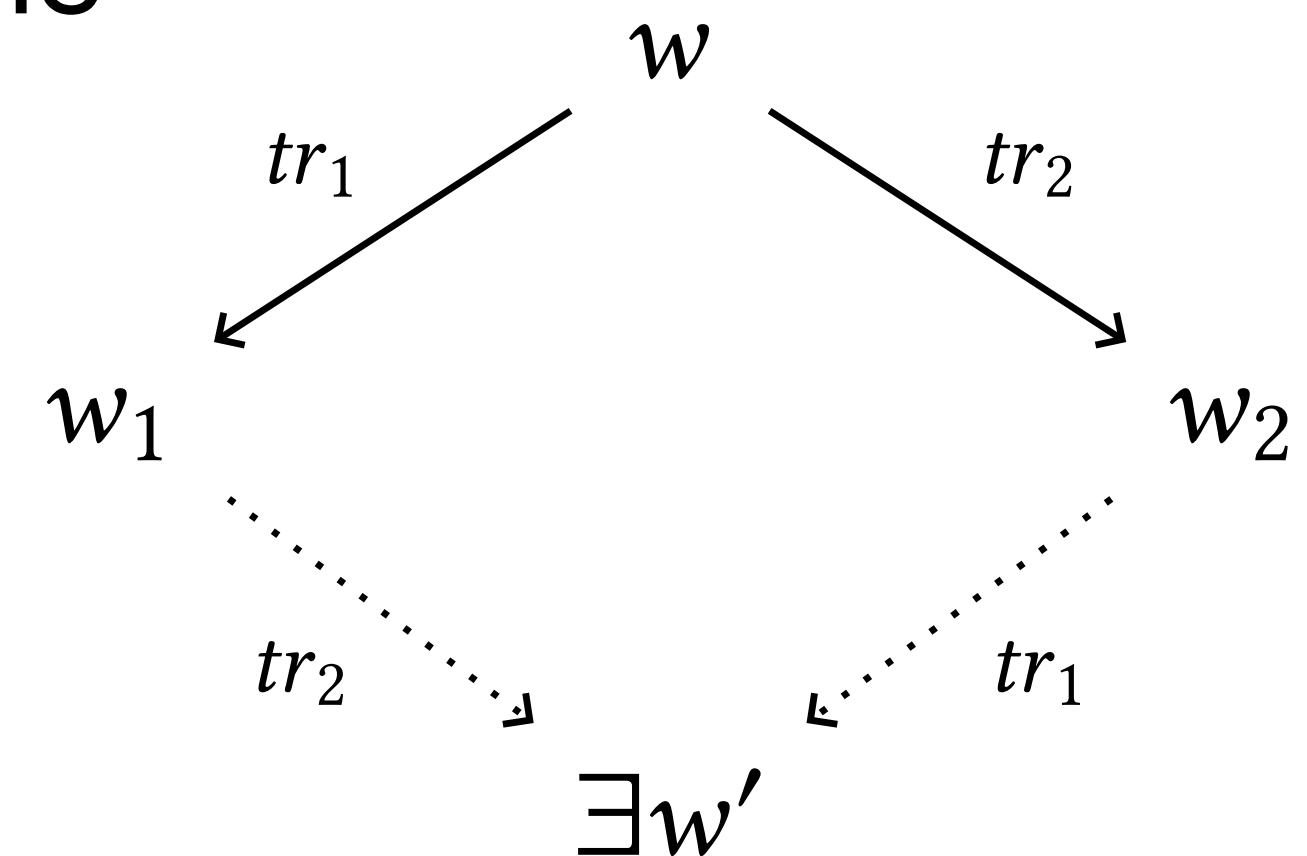
- *Well-synchronized* choreography simulates fully sequential choreography

# Ideal Simulates Sequential

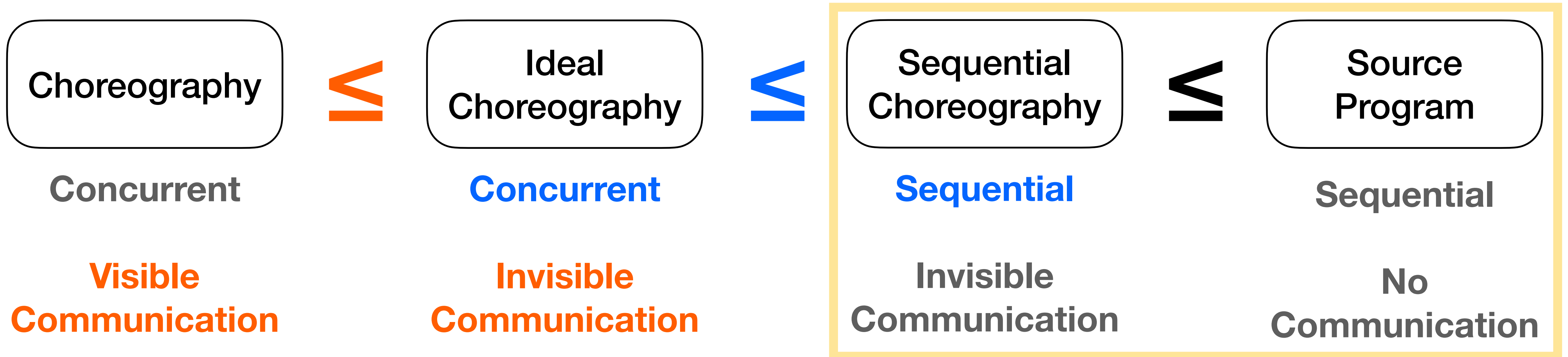
- *Well-synchronized* choreography simulates fully sequential choreography
- Two choreographies can fall out of sync, but remain joinable:
  - They only differ by internal actions
  - They can perform the same output at the same time

# Ideal Simulates Sequential

- *Well-synchronized* choreography simulates fully sequential choreography
- Two choreographies can fall out of sync, but remain joinable:
  - They only differ by internal actions
  - They can perform the same output at the same time
- Proved via confluence and a diamond lemma



# Dropping Host Annotations (Bookkeeping)



# Host Annotations Don't Do Anything

**Ideal, Sequential  
Choreography**

```
val x@Alice = e  
Alice.x ↗ Bob.y  
Bob.output(y)
```

**≅**

**Source Program**

```
val x = e  
Bob.output(x)
```



# Host Annotations Don't Do Anything

Ideal, Sequential  
Choreography

```
val x@Alice = e  
Alice.x ↗ Bob.y  
Bob.output(y)
```

≅

Source Program

```
val x = e  
Bob.output(x)
```

Internal step



# Host Annotations Don't Do Anything

Ideal, Sequential  
Choreography

```
val x@Alice = e  
Alice.x ↗ Bob.y  
Bob.output(y)
```

≅

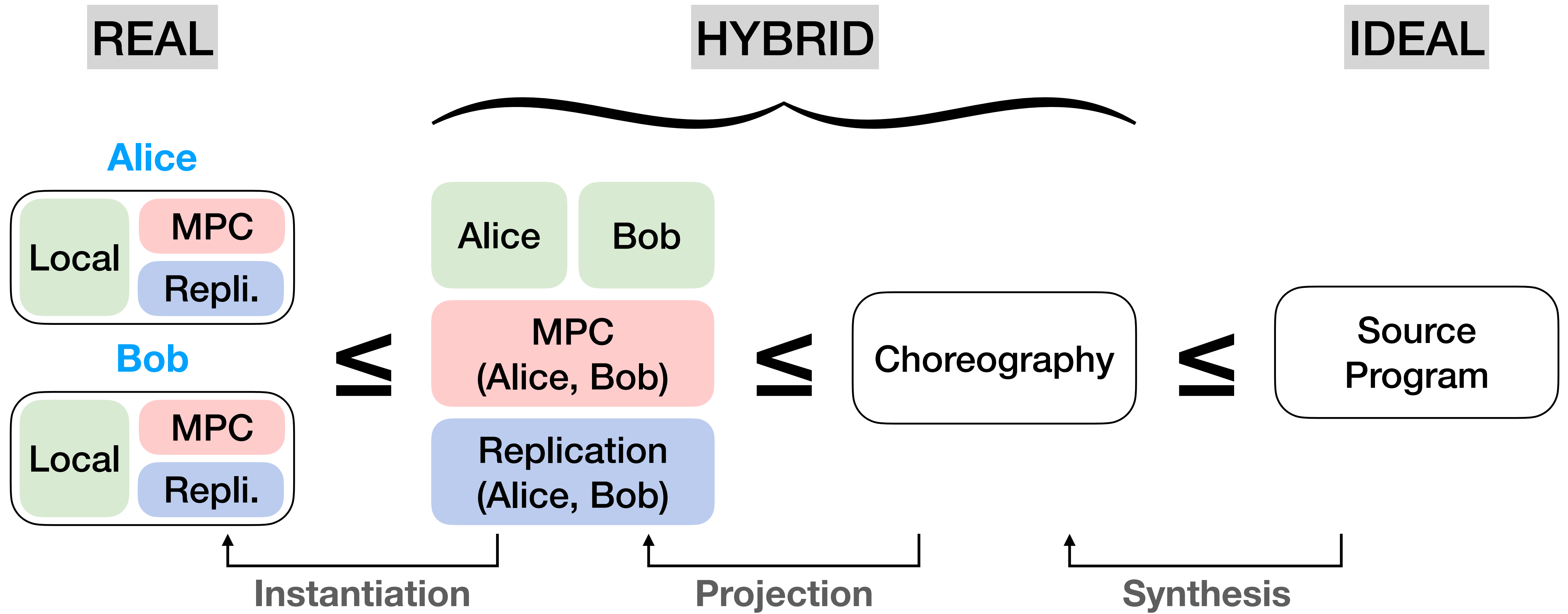
Source Program

```
val x = e  
Bob.output(x)
```

Internal step

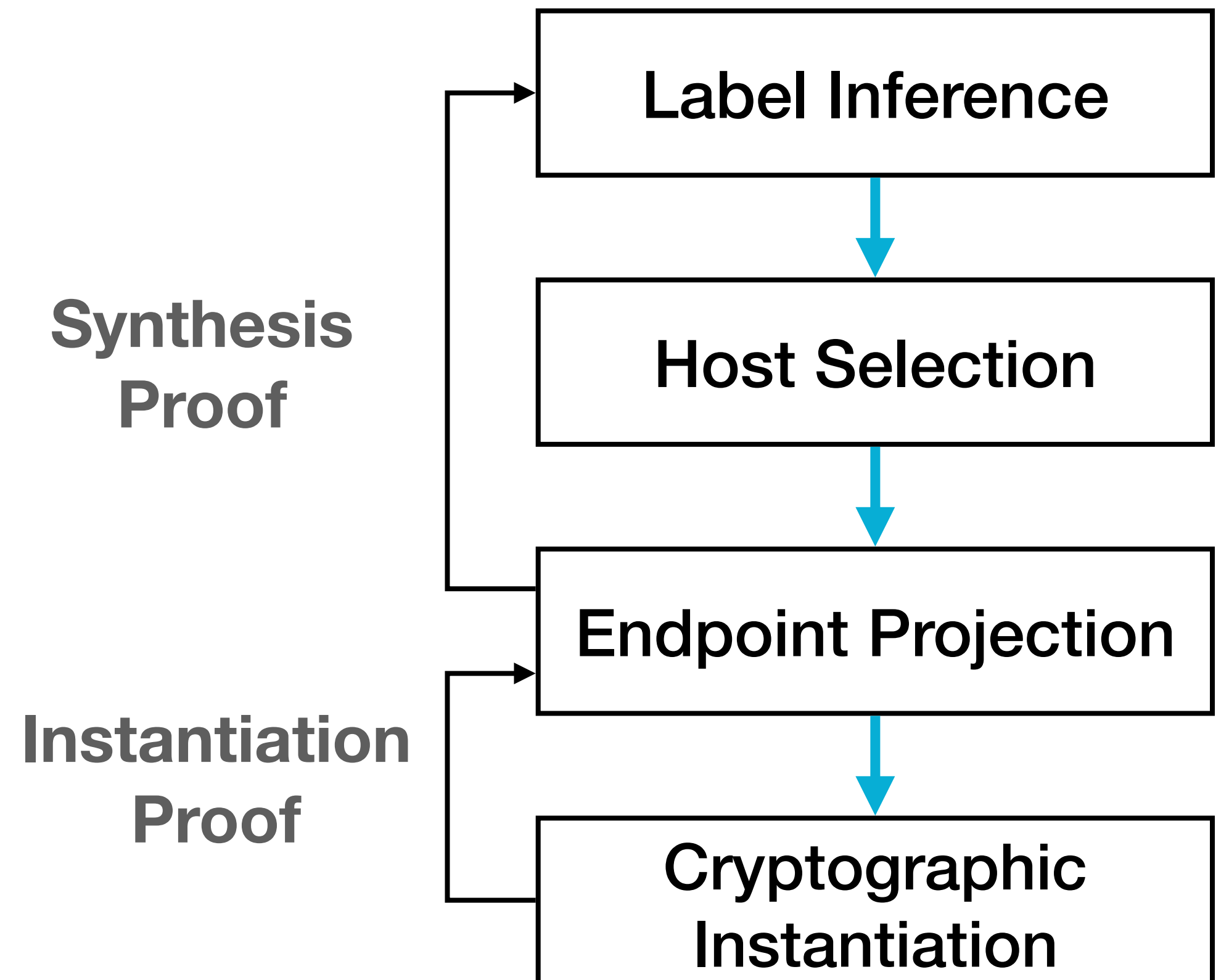
Only differ in number of internal steps.

# Proof Summary



# Conclusion

- Model cryptographic primitives as ideal hosts
- **Data labels** capture security **requirements**
- **Host labels** capture security **guarantees**
- **Choreographies** simplify distributed reasoning
- UC allows **separate proofs** for protocol synthesis and cryptographic instantiation
- UC simulation implies a strong compiler correctness condition (RHP)



[viaduct-lang.org](http://viaduct-lang.org)